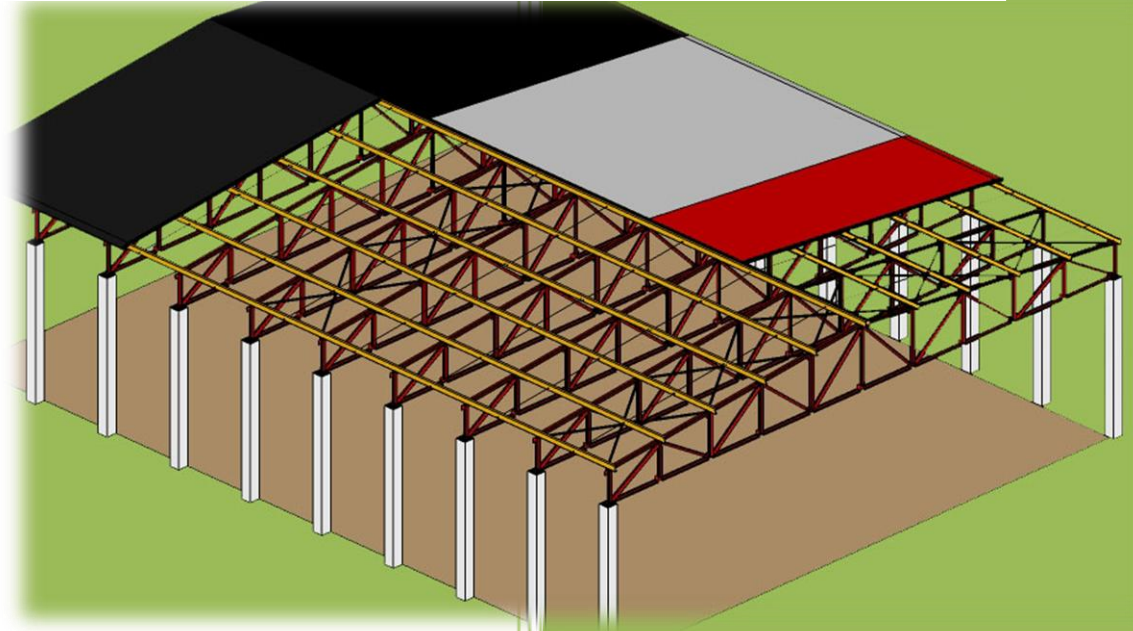




2011

# STEEL STRUCTURAL PROJECT (ROOF TRUSS)



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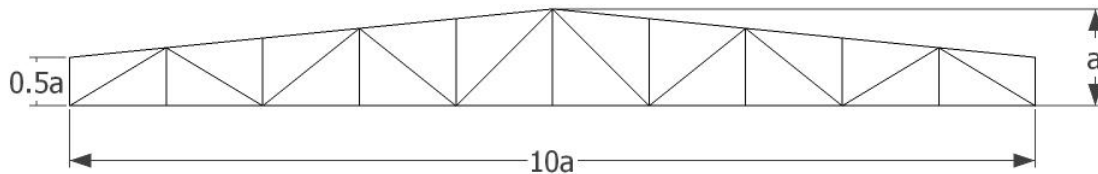
عادل علي حسن هرمس 2008/221

### The project

A garage consist of ( $n=10$ ) trusses, (type as has been selected for each group of students), each spaced ( $s$ ) m. The roof trusses are supported by concrete columns  $10 \times a$  m apart. Estimate the dead load on the truss and use snow load of  $1.2 \text{ kN/m}^2$  of horizontal projection and wind load of  $0.5 \text{ kN/m}^2$  on leeward side and  $0.25 \text{ kN/m}^2$  on the windward side and roofing of  $1.0 \text{ kN/m}^2$ .

### Design Data

1. A36 steel.
2. Type of connections: welded for left hand bolted connections for right hand side half. (assume all connection are bolted for member design)



### Requirement

1. Draw to scale 1:100 general arrangements showing all structural elements.
2. Calculate different load acting on an intermediate truss.
3. Determine the design force in each member (table format).
4. Design each section (Find suitable section for chord and web members).
5. Design half of the joints as welded connections and the other as bolted connections.
6. Study the system of bracing for the building.

*For our project:*

*$s = 4m, a = 2.8m$*

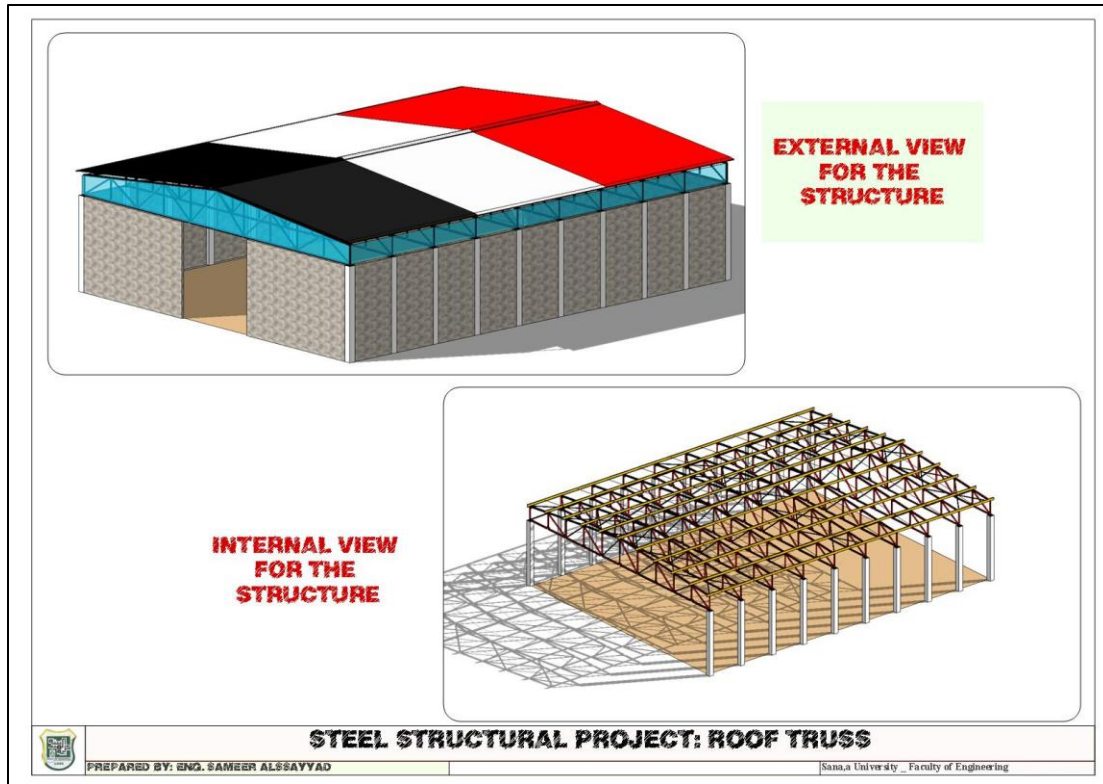


Fig. (1)

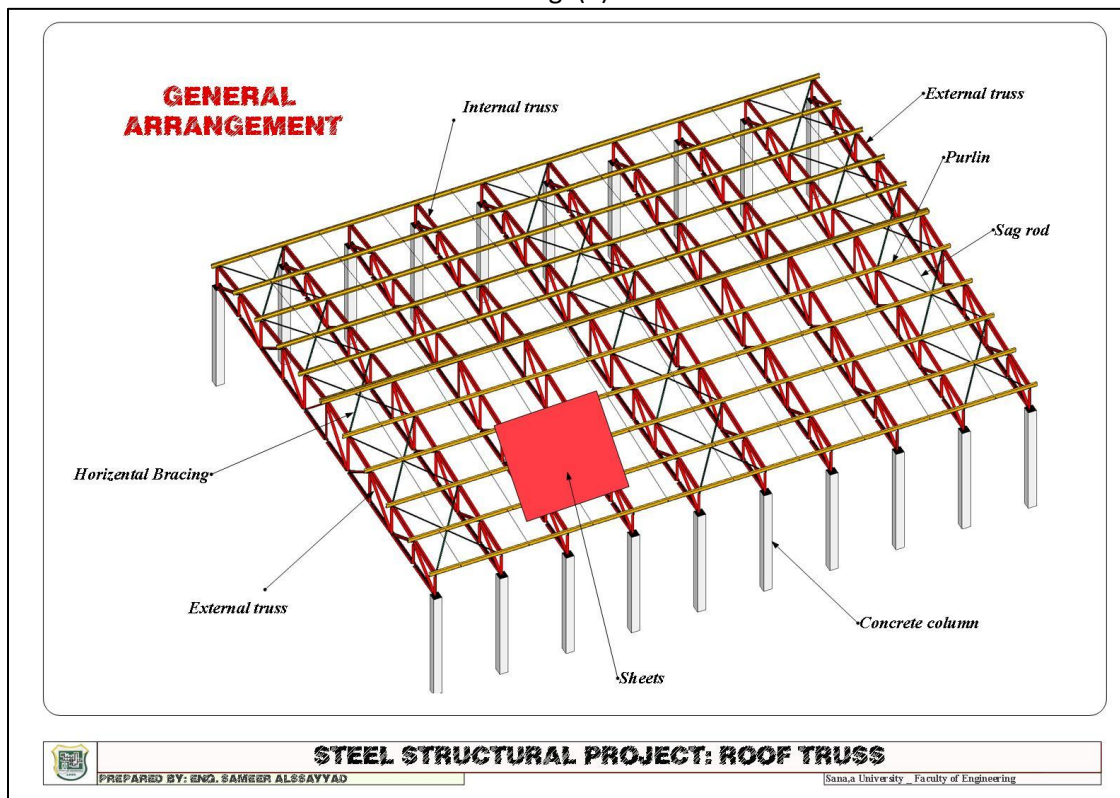


Fig. (2)

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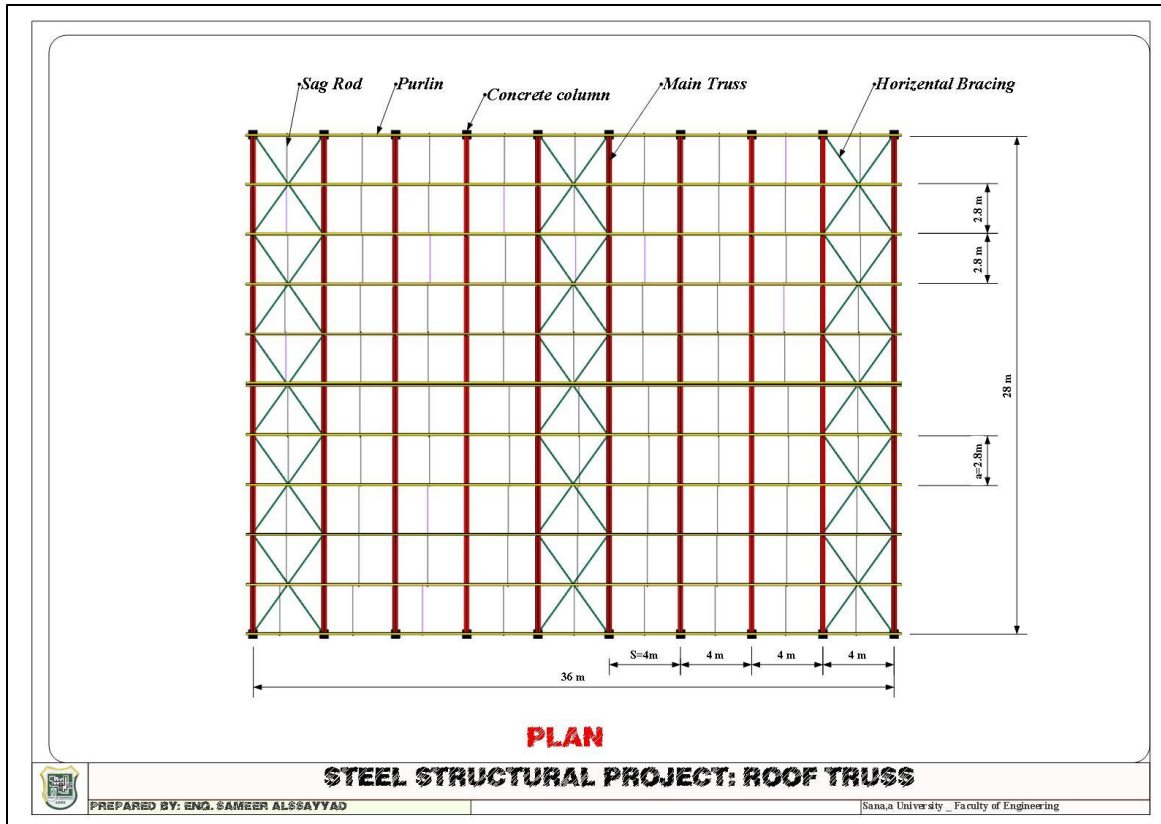


Fig. (3)

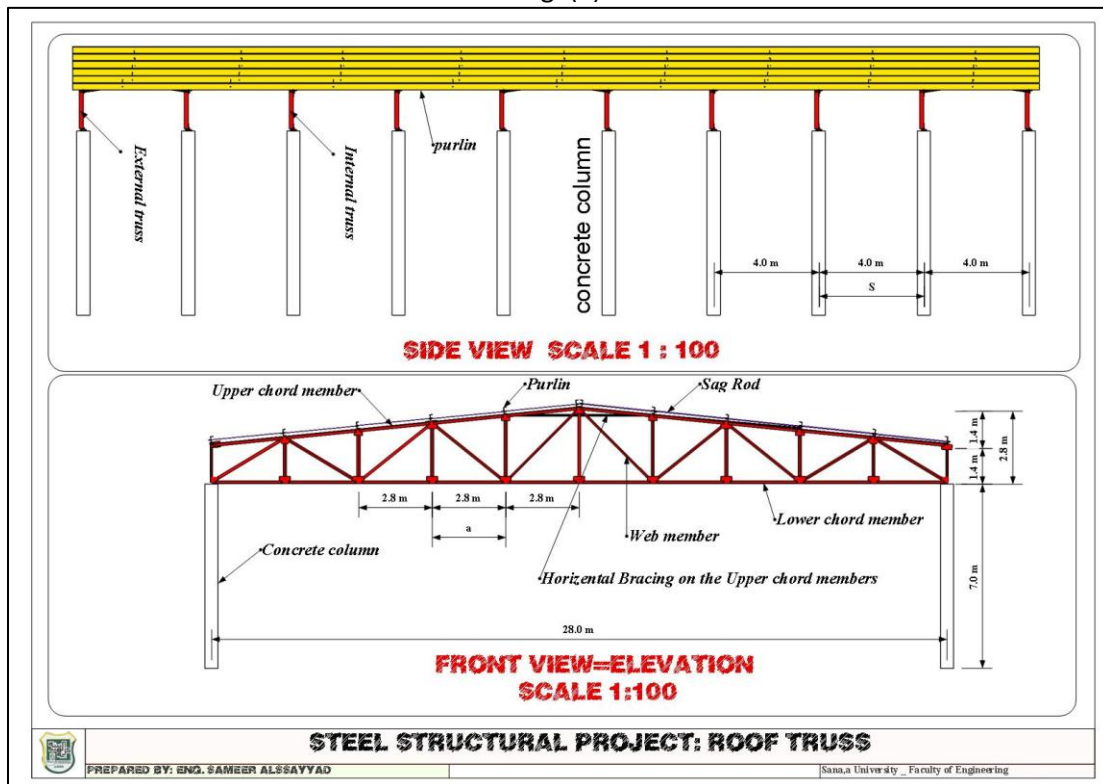


Fig.(4)

From figure 1 to figure 4 are show the general arrangement of the building.

### Calculation of loads acting on an internal truss

#### *Live load*

From the ASCE 7-05 table (4-1) we take  $LL = 1 \text{ kN/m}^2$  which is on the horizontal projection.

Then  $LL = 1 \cos\theta = 0.995 \text{ kN/m}^2$  (on the inclined length and  $\theta = 5.710593137^\circ$ )

Load on internal nod in a typical internal truss equal  $0.995 * 4 * 2.8 = 11.144 \text{ kN/m}^2$

#### *Snow load*

As it given in our project  $1.2 \text{ kN/m}^2$  on the horizontal projection

Then  $SL = 1.2 \cos\theta = 1.194 \text{ kN/m}^2$  (on the inclined length and  $\theta = 5.710593137^\circ$ )

Load on internal nod in a typical internal truss equal  $1.194 * 4 * 2.8 = 13.373 \text{ kN/m}^2$

#### *Estimating Dead load*

The weight of the roof truss and its bracing is taken approximately 10% of the loading it is required to support.

We will take it due the live and snow loads as shown in the table

#### NOTE

The unit load analysis will use for calculate the live, snow and dead loads internal forces.

### Analysis of the truss using Joints method due to unit load

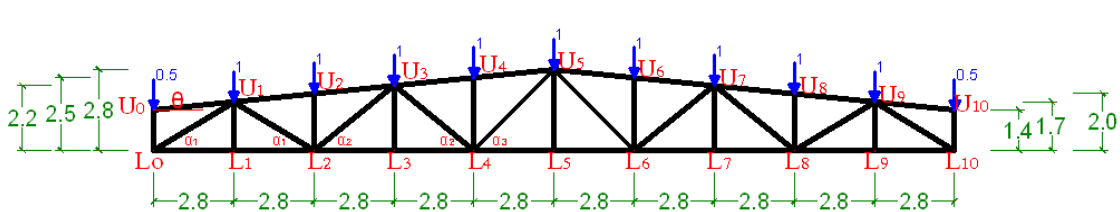
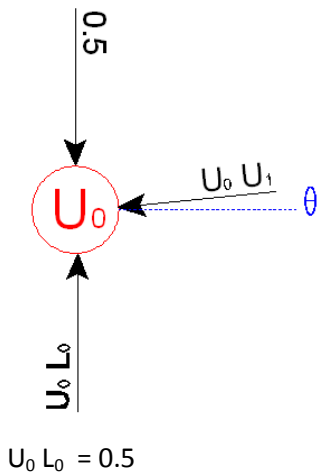


Fig. (5) Names of Joints and truss geometry

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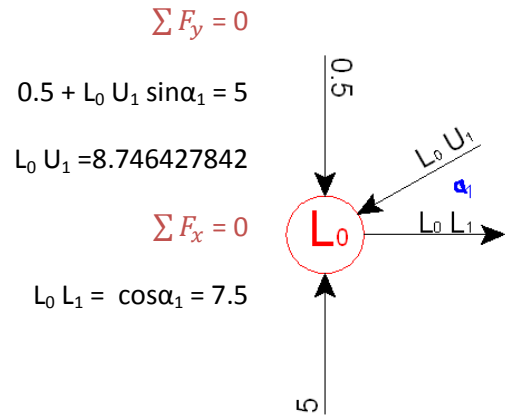


$$\sum F_x = 0$$

$$U_0 U_1 \cos\theta = 0$$

$$U_0 U_1 = 0$$

$$\sum F_y = 0$$

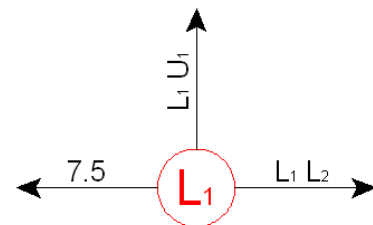


$$\sum F_x = 0$$

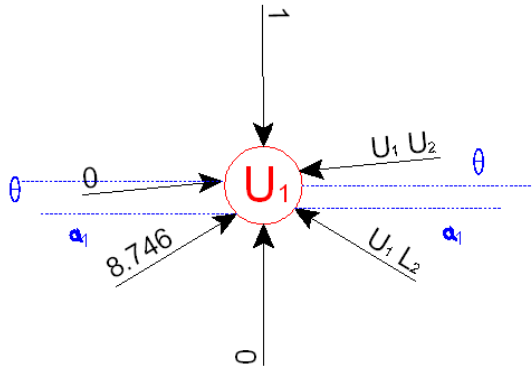
$$L_1 L_2 = 7.5$$

$$\sum F_y = 0$$

$$L_1 U_1 = 0$$



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$$\sum F_y = 0$$

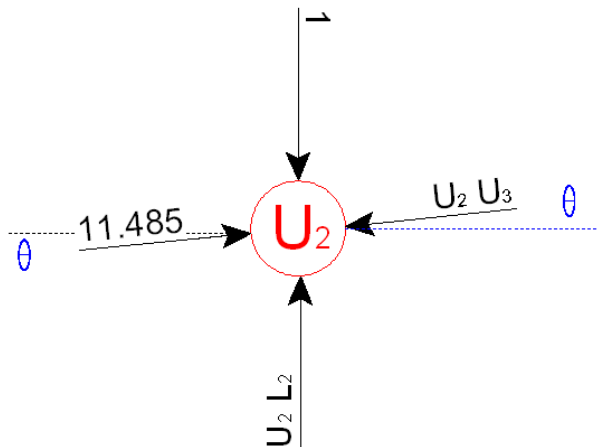
$$1 + U_1 U_2 \sin\theta = 8.746 \sin \alpha_1 + U_1 L_2 \sin \alpha_1$$

$$\sum F_x = 0$$

$$8.746 \cos \alpha_1 = U_1 L_2 \cos \alpha_1 + U_1 U_2 \cos\theta$$

$$U_1 U_2 = 11.48557214$$

$$U_1 L_2 = -4.581462203$$



$$\sum F_x = 0$$

$$U_2 U_3 = 11.48557214$$

$$\sum F_y = 0$$

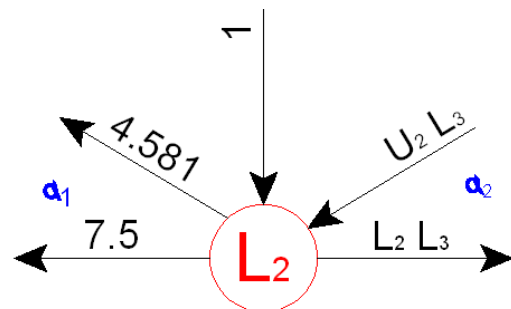
$$U_2 L_2 = 1$$

$$\sum F_y = 0 \rightarrow 1 + L_2 U_3 \sin\alpha_2 = 4.581 \sin\alpha_1$$

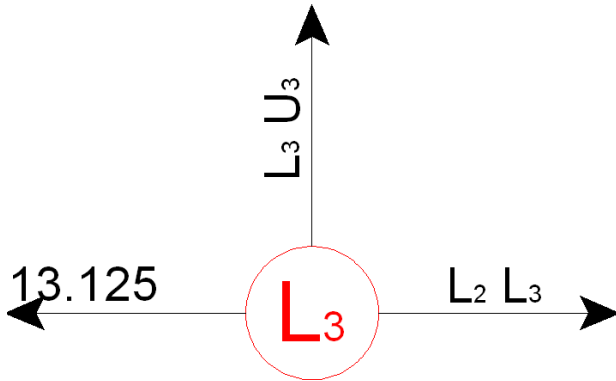
$$L_2 U_3 = 2.17248858$$

$$\sum F_x = 0 \rightarrow 7.5 + 4.581 \cos \alpha_1 + L_2 U_3 \cos\alpha_2 = L_2 L_3$$

$$L_2 L_3 = 13.125$$



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$$\sum F_x = 0$$

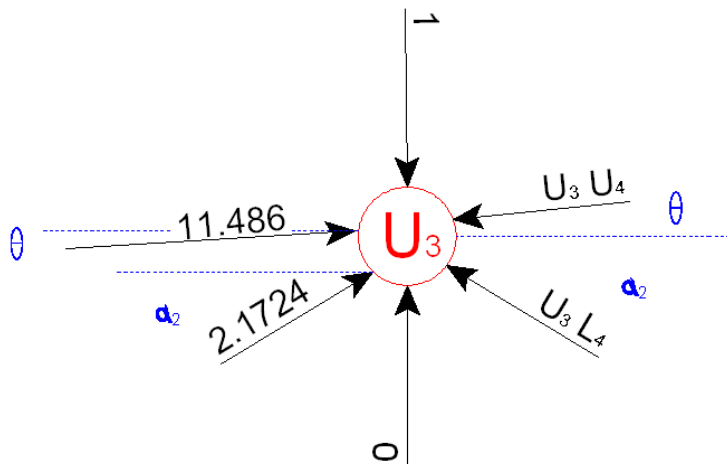
$$L_3 L_4 = 13.125$$

$$\sum F_y = 0$$

$$L_3 U_3 = 0$$

$$\sum F_x = 0$$

$$U_3 U_4 \cos\theta + U_3 L_4 \cos\alpha_2 = 11.4855 \cos\theta + 2.1724 \cos\alpha_2$$



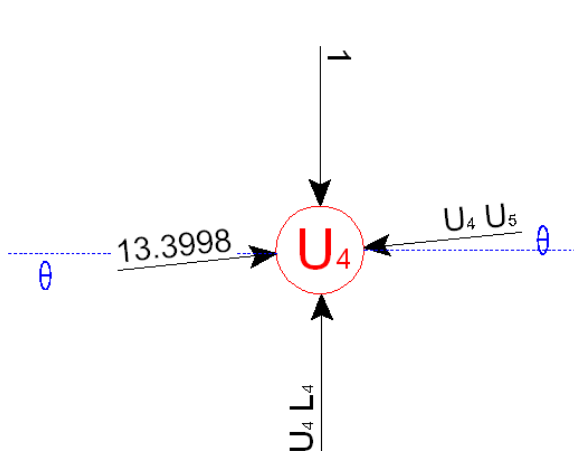
$$\sum F_y = 0$$

$$1 + U_3 U_4 \sin\theta = 2.175 \sin\alpha_2$$

$$+ U_3 L_4 \sin\alpha_2 + 11.4855 \sin\theta$$

$$U_3 U_4 = 13.39983416$$

$$U_3 L_4 = -0.2667968432$$



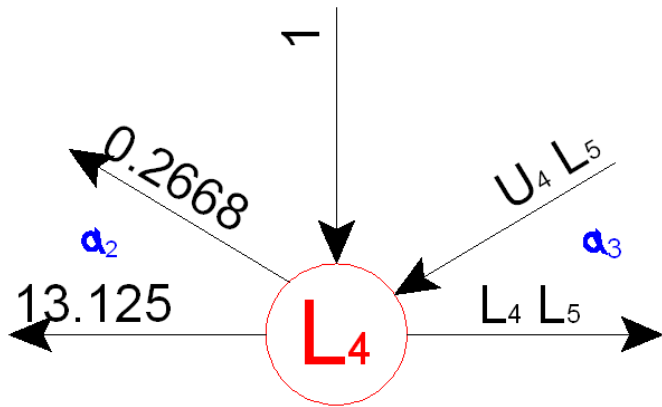
$$\sum F_x = 0$$

$$U_4 U_5 = 13.39983416$$

$$\sum F_y = 0$$

$$U_4 L_4$$





$$\sum F_y = 0$$

$$1 + L_4 U_5 \sin \alpha_3 =$$

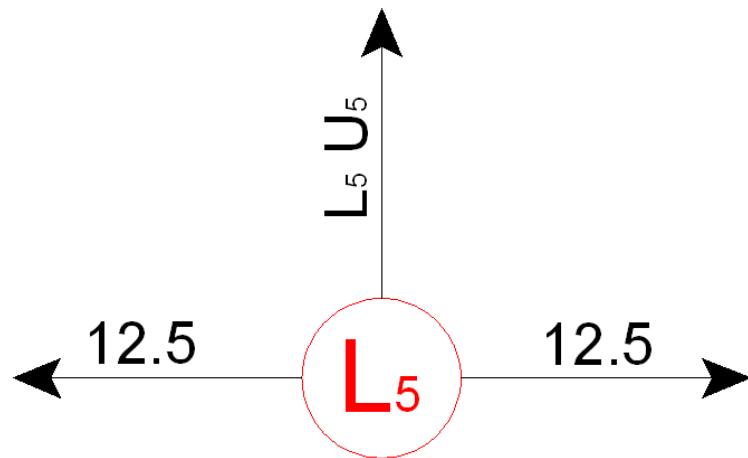
$$0.266797 \sin \alpha_2$$

$$L_4 U_5 = -1.178511302$$

$$\sum F_x = 0$$

$$13.125 + 1.266 \cos \alpha_2 + L_4 U_5 \cos \alpha_3 = L_4 L_5$$

$$L_4 L_5 = 12.5$$



$$\sum F_y = 0$$

$$L_5 U_5 = 0$$

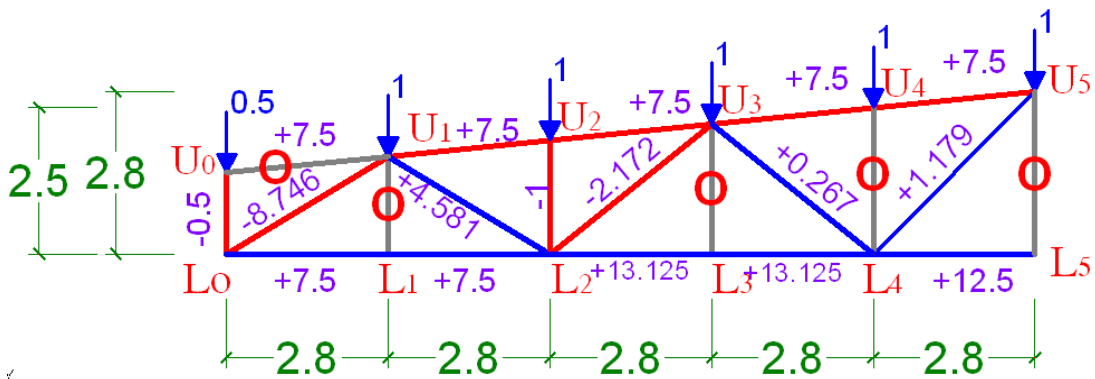
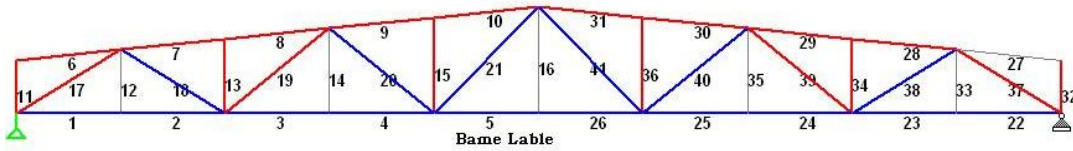


Fig. (6) Internal forces.

Fig. (7) Beams labels.



### Calculation of Wind Load

For the static approach, the fluctuating pressure caused by a constantly blowing wind is approximated by a mean velocity pressure that acts on the structure. This pressure  $q$  is defined by its kinetic energy,  $q = \frac{1}{2} \rho V^2$ ,

Where  $\rho$  is the density of the air and  $V$  is its velocity. According to the ASCE 7-05 Standard, this equation is modified to account for the importance of the structure, its height, and the terrain in which it is located. It is represented as

$$q_z = 0.613 K_z K_{zt} K_d V^2 I \quad (\text{N/m}^2) \quad (\text{ASCE 7-05 eq. 6-15})$$

Where,

$V$  = the velocity in m/s of a 3-second gust of wind measured 10 m above the ground during a 50-year recurrence period. Values are obtained from H. Althafere wind map of Yemen.

$I$  = the importance factor that depends upon the nature of the building occupancy; Values are obtained from ASCE 7-05 table (6-1)

$K_z$  = the velocity pressure exposure coefficient, which is a function of height and depends upon the ground terrain. Hibbeler 7th edition Table 1-5 lists values for a structure which is located in open terrain with scattered low-lying obstructions.

$K_{zt}$  = a factor that accounts for wind speed increases due to hills and escarpments. For fiat ground  $K_{zt} = 1$ .

$K_d$  = a factor that accounts for the direction of the wind. It is used only when the structure is subjected to combinations of loads Values are obtained from ASCE 7-05 table (6-4)

Table of Velocity pressure Exposure Coefficient for Terrain with Low-Lying Obstructions	
$z$ (m)	$K_z$
0 – 4.6	0.85
6.1	0.90
7.6	0.94
9.1	0.98
12.2	1.04
15.2	1.09

**Design Wind Pressure for Enclosed Buildings.** Once the value for  $q_z$  is obtained, the design pressure can be determined from a list of relevant equations listed in the ASCE 7-05 Standard. The choice depends upon the flexibility and height of the structure, and whether the design is for the main wind-force resisting system, or for the building's components and cladding. For example, for a conservative design wind-pressure on nonflexible buildings of any height is determined using a two-termed equation -resulting from both external and internal pressures, namely,

$$P = q G C_p - q_h (GC_{pi})$$

(ASCE 7-05 eq. 6-19)

Here

$q = q_z$  for the windward wall at height  $z$  above the ground (last Eq.), and  $q = q_h$  for the leeward walls, side walls, and roof, where  $z = h$ , the mean height of the roof.

$G$  = a wind-gust effect factor, which depends upon the exposure. For example, for a rigid structure,

$G = 0.85$ .

$C_p$  = a wall or roof pressure coefficient determined from ASCE 7-05 table (6-1).

$(GC_{pi})$  = the internal pressure coefficient which depends upon the type of openings in the building. For fully enclosed buildings  $(GC_{pi}) = \pm 0.18$  ASCE 7-05 figure (6-5). Here the signs indicate that either positive or negative (suction) pressure can occur within the building.

Table (1)

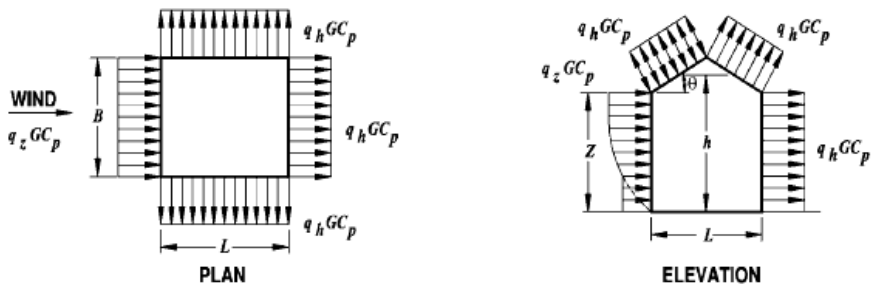
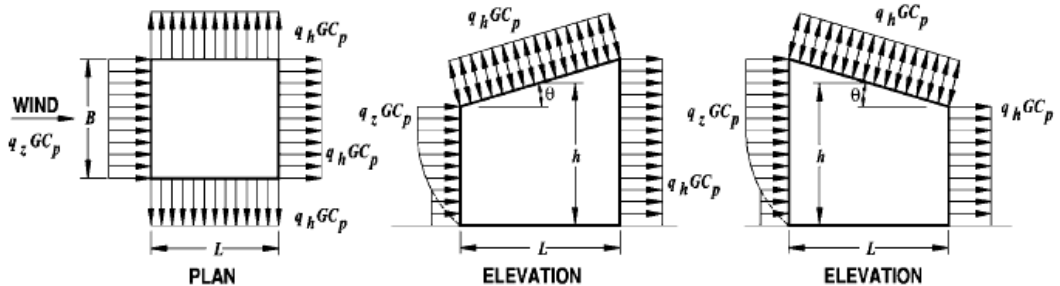
Main Wind Force Resisting System – Method 2		All Heights
Figure 6-6	External Pressure Coefficients, $C_p$	Walls & Roofs
Enclosed, Partially Enclosed Buildings		
 <p style="text-align: center;"><b>GABLE, HIP ROOF</b></p>		
 <p style="text-align: center;"><b>MONOSLOPE ROOF (NOTE 4)</b></p>		

Table (2)

Main Wind Force Resisting System – Method 2										All Heights		
Figure 6-6 (con't)		External Pressure Coefficients, $C_p$								Walls & Roofs		
Enclosed, Partially Enclosed Buildings												
Wall Pressure Coefficients, $C_p$												
Surface		L/B		$C_p$		Use With						
Windward Wall		All values		0.8		$q_z$						
Leeward Wall		0-1		-0.5		$q_h$						
		2		-0.3								
		$\geq 4$		-0.2								
Side Wall		All values		-0.7		$q_h$						
Roof Pressure Coefficients, $C_p$ , for use with $q_h$												
Wind Direction	Windward										Leeward	
	Angle, $\theta$ (degrees)											
	h/L	10	15	20	25	30	35	45	$\geq 60^\#$	10	15	$\geq 20$
Normal to ridge for $\theta \geq 10^\circ$	$\leq 0.25$	-0.7 -0.18	-0.5 0.0*	-0.3 0.2	-0.2 0.3	-0.2 0.3	0.0* 0.4	0.4	0.01 $\theta$	-0.3	-0.5	-0.6
	0.5	-0.9 -0.18	-0.7 -0.18	-0.4 0.0*	-0.3 0.2	-0.2 0.2	-0.2 0.3	0.0* 0.4	0.01 $\theta$	-0.5	-0.5	-0.6
	$\geq 1.0$	-1.3** -0.18	-1.0 -0.18	-0.7 -0.18	-0.5 0.0*	-0.3 0.2	-0.2 0.2	0.0* 0.3	0.01 $\theta$	-0.7	-0.6	-0.6
Normal to ridge for $\theta < 10^\circ$ and	$\leq 0.5$	Horiz distance from windward edge			$C_p$		*Value is provided for interpolation purposes. **Value can be reduced linearly with area over which it is applicable as follows					
		0 to h/2			-0.9, -0.18							
		h/2 to h			-0.9, -0.18							
		h to 2h			-0.5, -0.18							
Parallel to ridge for all $\theta$	$\geq 1.0$	0 to h/2			-1.3**, -0.18		Area (sq ft)		Reduction Factor			
		> h/2			-0.7, -0.18		$\leq 100$ (9.3 sq m)		1.0			
							200 (23.2 sq m)		0.9			
					$\geq 1000$ (92.9 sq m)		0.8					
<b>Notes:</b>												
1. Plus and minus signs signify pressures acting toward and away from the surfaces, respectively.												
2. Linear interpolation is permitted for values of L/B, h/L and $\theta$ other than shown. Interpolation shall only be carried out between values of the same sign. Where no value of the same sign is given, assume 0.0 for interpolation purposes.												
3. Where two values of $C_p$ are listed, this indicates that the windward roof slope is subjected to either positive or negative pressures and the roof structure shall be designed for both conditions. Interpolation for intermediate ratios of h/L in this case shall only be carried out between $C_p$ values of like sign.												
4. For monoslope roofs, entire roof surface is either a windward or leeward surface.												
5. For flexible buildings use appropriate $G_f$ as determined by Section 6.5.8.												
6. Refer to Figure 6-7 for domes and Figure 6-8 for arched roofs.												
7. Notation:												
B: Horizontal dimension of building, in feet (meter), measured normal to wind direction.												
L: Horizontal dimension of building, in feet (meter), measured parallel to wind direction.												
h: Mean roof height in feet (meters), except that eave height shall be used for $\theta \leq 10$ degrees.												
z: Height above ground, in feet (meters).												
G: Gust effect factor.												
$q_z, q_h$ : Velocity pressure, in pounds per square foot ( $N/m^2$ ), evaluated at respective height.												
$\theta$ : Angle of plane of roof from horizontal, in degrees.												
8. For mansard roofs, the top horizontal surface and leeward inclined surface shall be treated as leeward surfaces from the table.												
9. Except for MWFRS's at the roof consisting of moment resisting frames, the total horizontal shear shall not be less than that determined by neglecting wind forces on roof surfaces.												
#For roof slopes greater than $80^\circ$ , use $C_p = 0.8$												

*For our project*

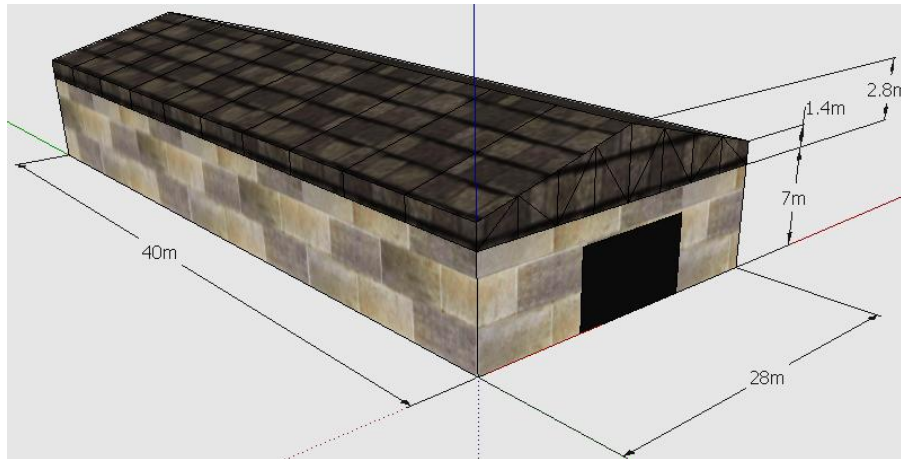


Fig. (8)

$V = 95 \text{ km/hr}$  or  $26.389 \text{ m/s}$   
 $I = 1.0$  from ASCE 7-05 table 6-1 class 2  
 $K_{zt} = 1.0$  assuming flat ground  
 $K_d = 0.85$  from ASCE 7-05 table 6-4

$$q_z = 0.613 K_z K_{zt} K_d V^2 I \text{ (N/m}^2\text{)} \quad (\text{ASCE 7-05 eq. 6-15})$$

$q_z = 0.613 * K_z * 1.0 * 0.85 * 26.389^2 * 1.0$   
 $= 362.845 * K_z$   
 $h = 7\text{m} + 2.8\text{m}$  (because  $\theta < 10 \text{ deg.}$ )

Table (3)

Z (m)	$K_z$	$q_z \text{ (N/m}^2\text{)}$
0-4.6	0.85	308.42
6.1	0.9	326.56
7.6	0.94	341.07
9.1	0.98	355.59
<b>h=9.8</b>	0.999	362.36

$$P = q G C_p - q_h (GC_{pi})$$
$$= q * 0.85 * C_p - 362.36(-+0.18)$$
$$= 0.85 * q * C_p - \&+ 65.22$$

*Windward Wall*

From  $z=7\text{m}$  to  $8.4\text{m}$  ( $C_p=0.8$ ,  $q=q_z$ )  
 $q_{7-8.4} = 166.71 \text{ N/m}^2$  or  $297.15 \text{ N/m}^2$

*Leeward Wall*

$L/B = 28/40 = 0.7$

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then  $C_p = -0.5$ ,  $q = q_h$   
 $p = -219.22 \text{ N/m}^2$  or  $-88.78 \text{ N/m}^2$

**Roof**

according to  $\Theta = 5.7106 < 10^\circ$

First value:

- $C_p = -0.9$  for distance 0 to  $h$
- $C_p = -0.5$  for distance  $h$  to  $2h$
- $C_p = -0.3$  for distance  $> 2h$

Second value:

- $C_p = -0.18$  for distance 0 to end.

When  $C_p = -0.9$  then  $p = -342.43 \text{ N/m}^2$  or  $-211.99 \text{ N/m}^2$

When  $C_p = -0.5$  then  $p = -219.22 \text{ N/m}^2$  or  $-88.78 \text{ N/m}^2$

When  $C_p = -0.3$  then  $p = -157.62 \text{ N/m}^2$  or  $-27.18 \text{ N/m}^2$

When  $C_p = -0.18$  then  $p = -120.66 \text{ N/m}^2$  or  $9.77 \text{ N/m}^2$

The load cases are showing in figure 9.

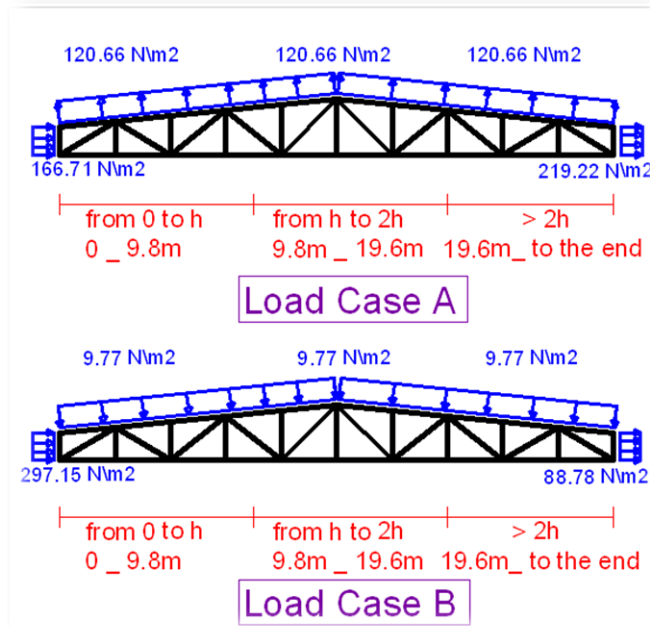


Fig. (9)

Here we will apply the loads for both cases in the two directions (from the left and from the right) as shown here.

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**Load case A**

Applying wind load from the left as showing in figure 10

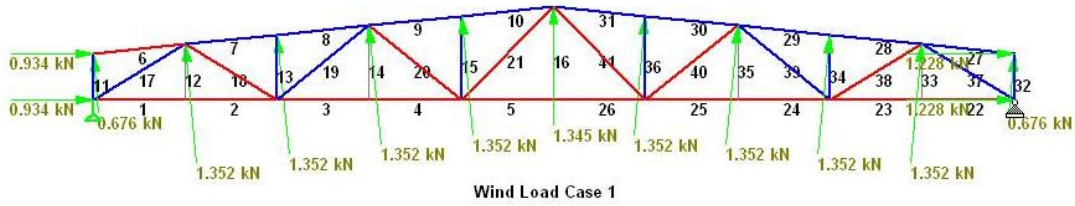


Fig. (10)

Applying wind load from the right as showing in figure 11

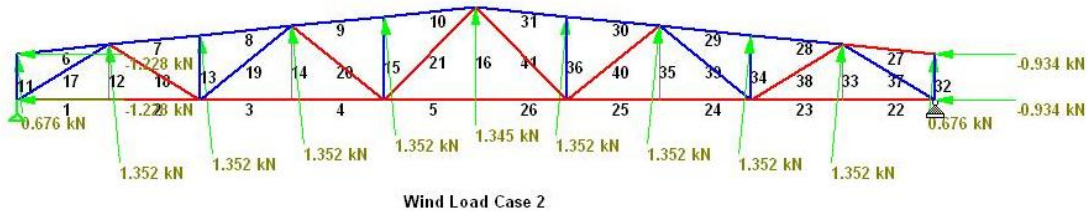


Fig. (11)

**Load case B**

Applying wind load from the left as showing in figure 12

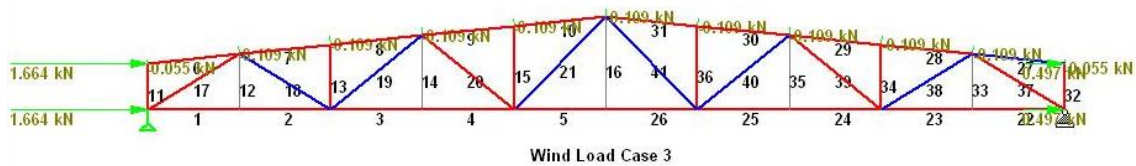


Fig. (12)

Applying wind load from the right as showing in figure 13

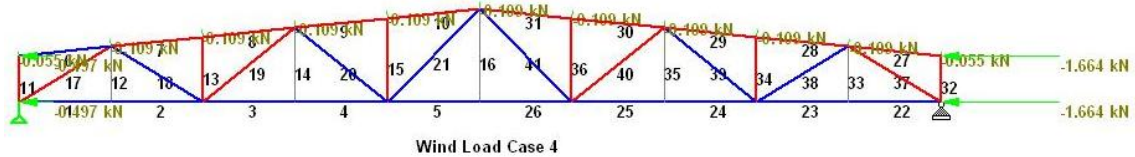


Fig. (13)

to analysis the truss due to load cases we will use the graphical method using computer program like Auto CAD as shown with load case 1 and the other we will use structural analysis program like STAAD Pro, The values of internal force writer in table 4. Labeling of spaces between forces figure 14.

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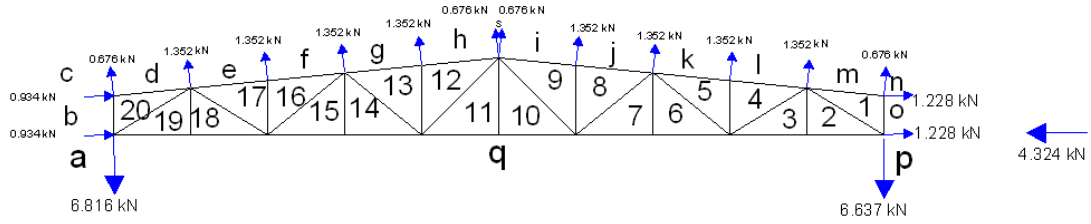


Fig. (14)

Drawing the graph figure 15.

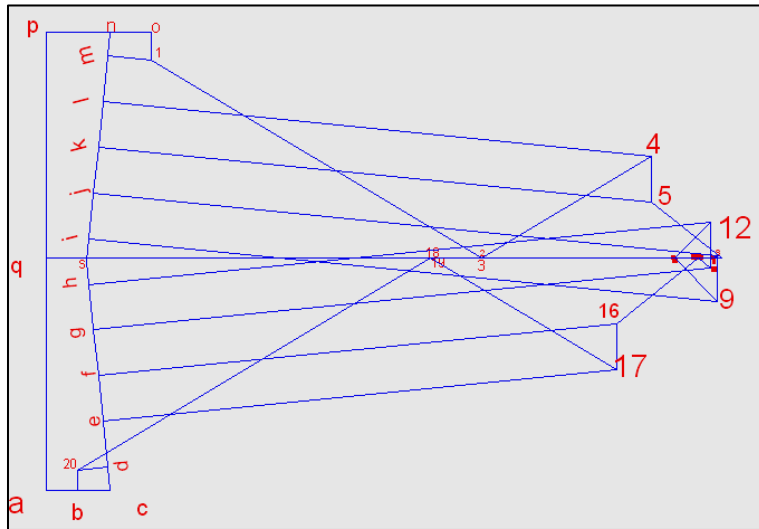


Fig. (15)

The loads due to load case 1 are shown in figure 16. (Red members for compression and blue members for tension member for all figures in this project)

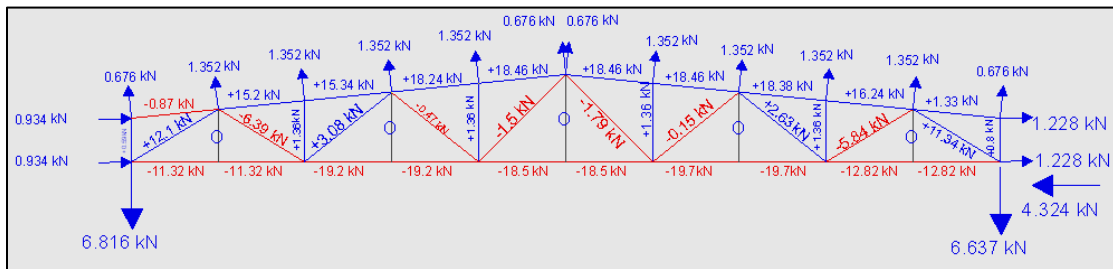


Fig. (16)



## Design of Purlins

### *Calculation of load per 1m*

#### **Live Load**

$L = 1 \text{ kN/m}^2$  ASCE 7-05 table (4-1) on the horizontal projection.

$L = 1 \cos\theta = 0.995 \text{ kN/m}^2$  on inclined length.

Live load on internal purlin =  $0.995 * 2.8 = 2.786 \text{ kN/m}$ .

#### *Snow Load*

$S = 1.2 \text{ kN/m}^2$  on the horizontal projection.

$L = 1.2 \cos\theta = 1.194 \text{ kN/m}^2$  on inclined length.

Snow load on internal purlin =  $1.194 * 2.8 = 3.343 \text{ kN/m}$ .

#### *Roofing Load*

In general roofing load taken between  $(0.3 - 1.0) \text{ kN/m}^2$ , in our project we will take it  $0.575 \text{ kN/m}^2 \rightarrow 0.575 * 2.8 = 1.609 \text{ kN/m}$  on purlin  $\rightarrow 1.609 * 4 = 6.436 \text{ kN}$  on nod

Roofing load per unit length on internal truss =  $0.575 * 2.8 = 1.609 \text{ kN/m}$ .

#### *Wind Load*

The critical wind load is load case B, then  $W = 9.77 * 10^{-3} * 2.8 = 0.027 \text{ kN/m}$ .

#### *Load Combinations*

- ❖  $w_{ux} = \{ (1.2) * (1.609) + (1.6) * (2.786) + (0.5) * (3.343) \} \cos\theta = 8.020 \text{ kN/m}$ .
- ❖  $w_{ux} = \{ (1.2) * (1.609) + (1.6) * (3.343) + (0.5) * (2.786) \} \cos\theta = \underline{8.630 \text{ kN/m}}$   
or =  $\{ (1.2) * (1.609) + (1.6) * (3.343) \} \cos\theta + (0.8) * (0.027) = 7.265 \text{ kN/m}$ .
- ❖  $w_{ux} = \{ (1.2) * (1.609) + (0.5) * (2.786) + (0.5) * (3.343) \} \cos\theta + 1.6 * 0.027 = 5.014 \text{ kN/m}$ .

$$M_{ux} = \frac{w_{ux} * l^2}{8} = \frac{8.630 * 4^2}{8} = 17.26 \text{ kN.m}$$

$$w_{uy} = \{ (1.2) * (1.609) + (1.6) * (3.343) + (0.5) * (2.786) \} \sin\theta = 0.8630 \text{ kN/m}$$

$$M_{uy} = \frac{w_{uy} * l^2}{32} = \frac{0.863 * 4^2}{32} = 0.4315 \text{ kN.m}$$
 one sag rod is used in mid point of the purlin

Here we will use calculation to find the suitable cold rolled section then we will create table 4 to other sections to use it in the design as follow

Try C180x250

$$\text{Area} = 2.5 * (180 + 2 * 40 + 2 * 16) = 730 \text{ mm}^2$$

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$$Z_x = 2 * 2.5(90 * 45 + 40 * 88.75 + 16 * 82) = 44560 \text{ mm}^3$$

Distance from the inner face toward the back (x)

$$(2 * 2.5 * (40 + 16)) + 180X = 180(2.5 - X) \rightarrow X = 0.47222 \text{ mm}$$

$$Z_y = \{ \{ (2.5 - 0.47222)^2 * 180 / 2 \} + 2 * 2.5 \{ (40 * 20.47222) + (16 * (46.25 + 0.47222)) \} \} + \{ 180 / 2 * 0.47222^2 \} = 7822.36 \text{ mm}^3$$

$$w_{ux} = \{ (1.2) * (1.609 + 5.23 * 9.81 * 10^{-3}) + (1.6) * (3.343) + (0.5) * (2.786) \} \cos \theta = 8.691 \text{ kN/m}$$

$$w_{uy} = \{ (1.2) * (1.609 + 5.23 * 9.81 * 10^{-3}) + (1.6) * (3.343) + (0.5) * (2.786) \} \sin \theta = 0.8691 \text{ kN/m}$$

$$M_{ux} = \frac{w_{ux} * l^2}{8} = \frac{8.691 * 4^2}{8} = 17.382 \text{ kN.m}$$

$$M_{uy} = \frac{w_{uy} * l^2}{32} = \frac{0.8691 * 4^2}{32} = 0.435 \text{ kN.m}$$

$$M_{px} = 0.9 * 400 * 44560 * 10^{-6} = 16.042 \text{ kN.m}$$

$$M_{py} = 0.9 * 400 * 7822.36 * 10^{-6} = 2.8161 \text{ kN.m}$$

$$\frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \leq 1.0 \rightarrow \frac{17.382}{16.042} + \frac{0.435}{2.8161} = 1.238 \rightarrow \text{Try larger one using table}$$

Section	Weight (kg/m)	D (mm)	T (mm)	B (mm)	Area (mm <sup>2</sup> )	Zx (mm <sup>3</sup> )	Zy (mm <sup>3</sup> )	ΦM <sub>px</sub> (kN*m)	ΦM <sub>py</sub> (kN*m)
C180x150	3.40	180	1.5	45	444	27331.5	4887.7	9.839	1.7596
C180x200	4.48	180	2.0	45	588	36044	6385.8	12.976	2.2989
C180x250	5.56	180	2.5	45	730	44560	7822.361	16.042	2.8161
C210x150	3.93	210	1.5	45	489	34329	4910.582	12.358	1.7678
C210x200	5.23	210	2.0	45	648	45314	6426.114	16.313	2.3134
C210x250	6.54	210	2.5	45	805	56072.5	7884.792	20.186	2.8385
C258x150	4.79	258	1.5	60	606	52700.25	7908.401	18.972	2.8470
C258x200	6.38	258	2.0	60	804	69698	10385.63	25.091	3.7388
C258x250	7.98	258	2.5	60	1000	86413.75	12787.26	31.109	4.6034

Table (4)

Try C 210x250 weight = 6.54 kg/m

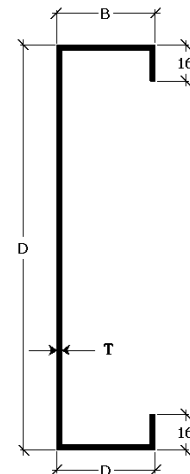
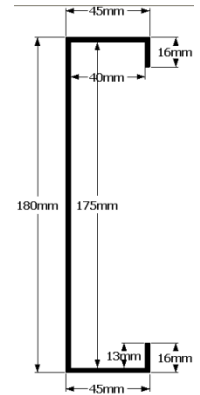
$$w_{ux} = \{ (1.2) * (1.609 + 6.54 * 9.81 * 10^{-3}) + (1.6) * (3.343) + (0.5) * (2.786) \} \cos \theta = 8.706 \text{ kN/m}$$

$$w_{uy} = \{ (1.2) * (1.609 + 6.54 * 9.81 * 10^{-3}) + (1.6) * (3.343) + (0.5) * (2.786) \} \sin \theta = 0.8706 \text{ kN/m}$$

$$M_{ux} = \frac{w_{ux} * l^2}{8} = \frac{8.706 * 4^2}{8} = 17.412 \text{ kN.m}$$

$$M_{uy} = \frac{w_{uy} * l^2}{32} = \frac{0.8706 * 4^2}{32} = 0.435 \text{ kN.m}$$

$$M_{px} = 20.186 \text{ kN.m}$$



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$$M_{py} = 2.8385 \text{ kN.m}$$

$$\frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \leq 1.0 \rightarrow \frac{17.412}{20.186} + \frac{0.435}{2.8385} = 1.0158 \rightarrow \text{Try lager one}$$

Try C258x150 weight = 4.79 kg/m

$$w_{ux} = \{ (1.2) * (1.609 + 4.79 * 9.81 * 10^{-3}) + (1.6) * (3.343) + (0.5) * (2.786) \} \cos\theta = 8.686 \text{ kN/m.}$$

$$w_{uy} = \{ (1.2) * (1.609 + 4.79 * 9.81 * 10^{-3}) + (1.6) * (3.343) + (0.5) * (2.786) \} \sin\theta = 0.8686 \text{ kN/m.}$$

$$M_{ux} = \frac{w_{ux} * l^2}{8} = \frac{8.686 * 4^2}{8} = 17.371 \text{ kN.m}$$

$$M_{uy} = \frac{w_{uy} * l^2}{32} = \frac{0.8686 * 4^2}{32} = 0.434 \text{ kN.m}$$

$$M_{px} = 18.972 \text{ kN.m}$$

$$M_{py} = 2.8470 \text{ kN.m}$$

$$\frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \leq 1.0 \rightarrow \frac{17.371}{18.972} + \frac{0.434}{2.847} = 1.068 \rightarrow \text{Try lager one}$$

Try C258x200 weight = 6.38 kg/m

$$w_{ux} = \{ (1.2) * (1.609 + 6.38 * 9.81 * 10^{-3}) + (1.6) * (3.343) + (0.5) * (2.786) \} \cos\theta = 8.704 \text{ kN/m.}$$

$$w_{uy} = \{ (1.2) * (1.609 + 6.38 * 9.81 * 10^{-3}) + (1.6) * (3.343) + (0.5) * (2.786) \} \sin\theta = 0.8704 \text{ kN/m.}$$

$$M_{ux} = \frac{w_{ux} * l^2}{8} = \frac{8.704 * 4^2}{8} = 17.409 \text{ kN.m}$$

$$M_{uy} = \frac{w_{uy} * l^2}{32} = \frac{0.8704 * 4^2}{32} = 0.4352 \text{ kN.m}$$

$$M_{px} = 25.091 \text{ kN.m}$$

$$M_{py} = 3.7388 \text{ kN.m}$$

$$\frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \leq 1.0 \rightarrow \frac{17.409}{25.091} + \frac{0.4352}{3.7388} = 0.810 \rightarrow \text{OK use C258x200}$$

$$\text{Loading on each nod of the truss} = (9.81 * 10^{-3} * 6.38) * 4 = 0.250 \text{ kN}$$

### Design of Sag Rod

Gravity load in  $\text{kN/m}^2$  of roof surface are as follows:

$$\text{Average weight in } \text{kN/m}^2 \text{ of the six purlin on each side of the roof} = \frac{6 * 0.06259}{14.0698} = 0.0267 \text{ kN/m}^2$$

$$\text{Live load} = 0.995 \text{ kN/m}^2$$

$$\text{Snow load} = 1.194 \text{ kN/m}^2$$

$$\text{Roofing} = 0.575 \text{ kN/m}^2$$

$$\text{Wind load} = 9.77 * 10^{-3} * \cos\theta = 0.0097 \text{ kN/m}^2$$

LRFD load on top inclined sag rod using controlling load factor equation

$$w_u = 1.2 * (0.0267 + 0.575) + 1.6 * 1.194 + 0.5 * 0.995 = 3.01299 \text{ kN/m}^2$$

$$\text{Component of load parallel to roof surface} = 3.01299 * \sin\theta = 0.3114 \text{ kN/m}^2$$

$$\text{Loading on top inclined sag rod} = (9/10) * (14.0698) * (6) * (0.3114) = 23.66 \text{ kN} = P_u$$

$$A_D = \frac{P_u}{\phi * 0.75 F_u} = \frac{23.66 * 1000}{0.75 * 0.75 * 400} = 105.17 \text{ mm}^2$$

Try (5/8-in) or (1.5 cm) rod as a minimum practical size 4 threads per 1cm  $A_D = 176.7 \text{ mm}^2$

$$R_n = 0.75 F_u A_D = 0.75 * 400 * 176.7 * 10^{-3} = 53.01 \text{ kN}$$

$$\phi R_n = 0.75 * 53.01 = 39.76 \text{ kN} > P_u \text{ OK}$$

Use 1.5cm

Check force in tie rod between ridge purlins

$$P_u = 14.0698 * 6 * 0.3114 * 1/\cos\theta = 26.42 \text{ kN} < 39.76 \text{ kN}$$

Use 1.5cm rod

## (ROOF TRUSS) Structural Steel Project

Table (5) Internal Forces.

Member	Unit Load	LL	SL	WL 1	WL 2	WL 3	WL 4	Max WL	Min WL	Roofing	purlin
1	7.5	83.6	100.3	-11.3	-8.5	-1.3	1.6	1.6	-11.3	48.3	1.9
2	7.5	83.6	100.3	-11.3	-8.5	-1.3	1.6	1.6	-11.3	48.3	1.9
3	13.125	146.3	175.5	-19.3	-15.5	-1.3	2.5	2.5	-19.3	84.5	3.3
4	13.125	146.3	175.5	-19.3	-15.5	-1.3	2.5	2.5	-19.3	84.5	3.3
5	12.5	139.3	167.2	-18.6	-14.3	-1.7	2.6	2.6	-18.6	80.5	3.1
6	0	0.0	0.0	-0.9	1.3	-1.7	0.5	1.3	-1.7	0.0	0.0
7	-11.486	-128.0	-153.6	15.3	16.2	-2.1	-1.2	16.2	-2.1	-73.9	-2.9
8	-11.486	-128.0	-153.6	15.4	16.3	-2.2	-1.2	16.3	-2.2	-73.9	-2.9
9	-13.4	-149.3	-179.2	18.3	18.6	-1.9	-1.7	18.6	-1.9	-86.2	-3.4
10	-13.4	-149.3	-179.2	18.5	18.7	-1.9	-1.7	18.7	-1.9	-86.2	-3.4
11	-0.5	-5.6	-6.7	0.6	0.8	-0.2	0.0	0.8	-0.2	-3.2	-0.1
13	-1	-11.1	-13.4	1.4	1.4	-0.1	-0.1	1.4	-0.1	-6.4	-0.3
15	-1	-11.1	-13.4	1.4	1.4	-0.1	-0.1	1.4	-0.1	-6.4	-0.3
17	-8.746	-97.5	-117.0	12.1	11.3	-0.4	-1.3	12.1	-1.3	-56.3	-2.2
18	4.581	51.1	61.3	-6.4	-5.8	0.1	0.7	0.7	-6.4	29.5	1.1
19	-2.172	-24.2	-29.0	3.1	2.6	0.1	-0.4	3.1	-0.4	-14.0	-0.5
20	0.267	3.0	3.6	-0.5	-0.1	-0.2	0.2	0.2	-0.5	1.7	0.1
21	1.179	13.1	15.8	-1.5	-1.8	0.3	0.0	0.3	-1.8	7.6	0.3
22	7.5	83.6	100.3	-12.8	-7.0	-2.7	3.0	3.0	-12.8	48.3	1.9
23	7.5	83.6	100.3	-12.8	-7.0	-2.7	3.0	3.0	-12.8	48.3	1.9
24	13.125	146.3	175.5	-19.8	-14.9	-1.8	3.0	3.0	-19.8	84.5	3.3
25	13.125	146.3	175.5	-19.8	-14.9	-1.8	3.0	3.0	-19.8	84.5	3.3
26	12.5	139.3	167.2	-18.6	-14.3	-1.7	2.6	2.6	-18.6	80.5	3.1
27	0	0.0	0.0	1.3	-0.9	0.5	-1.7	1.3	-1.7	0.0	0.0
28	-11.486	-128.0	-153.6	16.2	15.3	-1.2	-2.1	16.2	-2.1	-73.9	-2.9
29	-11.486	-128.0	-153.6	16.3	15.4	-1.2	-2.2	16.3	-2.2	-73.9	-2.9
30	-13.4	-149.3	-179.2	18.6	18.3	-1.7	-1.9	18.6	-1.9	-86.2	-3.4
31	-13.4	-149.3	-179.2	18.7	18.5	-1.7	-1.9	18.7	-1.9	-86.2	-3.4
32	-0.5	-5.6	-6.7	0.8	0.6	0.0	-0.2	0.8	-0.2	-3.2	-0.1
34	-1	-11.1	-13.4	1.4	1.4	-0.1	-0.1	1.4	-0.1	-6.4	-0.3
36	-1	-11.1	-13.4	1.4	1.4	-0.1	-0.1	1.4	-0.1	-6.4	-0.3
37	-8.746	-97.5	-117.0	11.3	12.1	-1.3	-0.4	12.1	-1.3	-56.3	-2.2
38	4.581	51.1	61.3	-5.8	-6.4	0.7	0.1	0.7	-6.4	29.5	1.1
39	-2.172	-24.2	-29.0	2.6	3.1	-0.4	0.1	3.1	-0.4	-14.0	-0.5
40	0.267	3.0	3.6	-0.1	-0.5	0.2	-0.2	0.2	-0.5	1.7	0.1
41	1.179	13.1	15.8	-1.8	-1.5	0.0	0.3	0.3	-1.8	7.6	0.3

## (ROOF TRUSS) Structural Steel Project

Table (6) Load combinations.

1.4D	1.2D+1.6L+5(Lr/S/R)	1.2D+1.6(Lr/S/R)+(.5Lor.8W)			1.2D+1.6W+5L+5(Lr/S/R)	1.2+1E+5L+2S	0.9D±(1.6Wor1E)		+ve Max Force (kN) Design	-ve Max Force (kN) Design	<i>Check for stress reversal</i>	Member
		A	B	C			A	B				
96.2	266.3	284.7	244.2	233.8	176.9	144.3	64.3	43.7	284.7	43.7	NA	1
96.2	266.3	284.7	244.2	233.8	176.9	144.3	64.3	43.7	284.7	43.7	NA	2
168.3	466.0	498.2	427.1	409.6	309.1	252.5	112.2	77.3	498.2	77.3	NA	3
168.3	466.0	498.2	427.1	409.6	309.1	252.5	112.2	77.3	498.2	77.3	NA	4
160.3	443.8	474.5	406.9	390.0	294.8	240.5	107.2	73.3	474.5	73.3	NA	5
0.1	0.1	0.1	1.1	-1.3	2.1	0.1	2.1	-2.6	2.1	-2.6	Reversal	6
-147.1	-407.7	-435.9	-358.9	-373.6	-241.0	-220.8	-68.7	-98.0	-68.7	-435.9	NA	7
-147.1	-407.7	-435.9	-358.8	-373.6	-240.8	-220.8	-68.5	-98.0	-68.5	-435.9	NA	8
-171.7	-475.7	-508.5	-419.0	-435.4	-281.7	-257.6	-80.6	-113.4	-80.6	-508.5	NA	9
-171.7	-475.7	-508.5	-418.9	-435.4	-281.5	-257.6	-80.4	-113.5	-80.4	-508.5	NA	10
-6.4	-17.7	-19.0	-15.5	-16.4	-10.3	-9.6	-2.8	-4.5	-2.8	-19.0	NA	11
-12.8	-35.5	-37.9	-31.3	-32.5	-21.1	-19.2	-6.1	-8.4	-6.1	-37.9	NA	13
-12.8	-35.5	-37.9	-31.3	-32.5	-21.1	-19.2	-6.1	-8.4	-6.1	-37.9	NA	15
-112.1	-310.5	-331.9	-273.5	-284.2	-183.8	-168.2	-52.6	-74.0	-52.6	-331.9	NA	17
58.7	162.6	173.9	148.9	143.2	107.6	88.1	38.9	27.5	173.9	27.5	NA	18
-27.8	-77.1	-82.4	-67.9	-70.7	-45.5	-41.8	-12.9	-18.6	-12.9	-82.4	NA	19
3.4	9.5	10.1	8.8	8.3	6.5	5.1	2.5	1.4	10.1	1.4	NA	20
15.1	41.8	44.7	38.4	36.7	27.9	22.7	10.3	6.8	44.7	6.8	NA	21
96.4	266.5	284.9	245.5	232.8	179.4	144.5	66.8	41.5	284.9	41.5	NA	22
96.4	266.5	284.9	245.5	232.8	179.4	144.5	66.8	41.5	284.9	41.5	NA	23
168.3	466.1	498.2	427.6	409.3	310.1	252.5	113.1	76.5	498.2	76.5	NA	24
168.3	466.1	498.2	427.6	409.3	310.1	252.5	113.1	76.5	498.2	76.5	NA	25
160.3	443.8	474.5	406.9	390.0	294.8	240.5	107.2	73.3	474.5	73.3	NA	26
-0.2	-0.2	-0.2	0.8	-1.5	1.9	-0.2	1.9	-2.8	1.9	-2.8	Reversal	27
-147.2	-407.8	-436.0	-359.0	-373.7	-241.1	-220.9	-68.8	-98.1	-68.8	-436.0	NA	28
-147.2	-407.8	-436.0	-358.9	-373.7	-240.9	-220.9	-68.5	-98.1	-68.5	-436.0	NA	29
-171.7	-475.7	-508.5	-419.0	-435.4	-281.7	-257.7	-80.6	-113.5	-80.6	-508.5	NA	30
-171.7	-475.7	-508.5	-418.9	-435.4	-281.5	-257.7	-80.4	-113.5	-80.4	-508.5	NA	31
-6.4	-17.8	-19.0	-15.6	-16.4	-10.4	-9.6	-2.8	-4.5	-2.8	-19.0	NA	32
-12.8	-35.5	-37.9	-31.3	-32.5	-21.1	-19.2	-6.1	-8.4	-6.1	-37.9	NA	34
-12.8	-35.5	-37.9	-31.3	-32.5	-21.1	-19.2	-6.1	-8.4	-6.1	-37.9	NA	36
-111.9	-310.4	-331.8	-273.4	-284.1	-183.7	-168.1	-52.5	-74.0	-52.5	-331.8	NA	37

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58.6	162.6	173.8	148.8	143.1	107.5	88.0	38.8	27.4	173.8	27.4	NA	38
-27.8	-77.1	-82.4	-67.8	-70.6	-45.5	-41.7	-12.9	-18.5	-12.9	-82.4	NA	39
3.4	9.4	10.1	8.7	8.2	6.4	5.1	2.4	1.4	10.1	1.4	NA	40
15.1	41.9	44.8	38.5	36.7	28.0	22.7	10.3	6.8	44.8	6.8	NA	41

Table (7) Final Internal forces.

	+ve Max Force (kN)	-ve Max Force (kN)	Type of force	Member	Length	Final design load (kN)
	Design	Design				
Lower Chord Members 2LBB	284.6941	43.66425	Tension	1	2.8	284.6941
	284.6941	43.66425	Tension	2	2.8	284.6941
	498.1851	77.33111	Tension	3	2.8	498.1851
	498.1851	77.33111	Tension	4	2.8	498.1851
	474.491	73.29334	Tension	5	2.8	474.491
	284.867	41.48674	Tension	22	2.8	284.867
	284.867	41.48674	Tension	23	2.8	284.867
	498.2499	76.51571	Tension	24	2.8	498.2499
	498.2499	76.51571	Tension	25	2.8	498.2499
474.491	73.29334	Tension	26	2.8	474.491	
Upper Chord Members 2LBB	2.14248	-2.64034	Reversal	6	2.814	Reversal
	-68.67	-435.856	Comp.	7	2.814	435.8559
	-68.455	-435.857	Comp.	8	2.814	435.8573
	-80.6214	-508.519	Comp.	9	2.814	508.5187
	-80.4048	-508.52	Comp.	10	2.814	508.52
	1.93218	-2.83582	Reversal	27	2.814	Reversal
	-68.7538	-435.968	Comp.	28	2.814	435.9677
	-68.5388	-435.969	Comp.	29	2.814	435.969
	-80.6431	-508.548	Comp.	30	2.814	508.5476
-80.4265	-508.549	Comp.	31	2.814	508.5489	
Web Members (One Angle)	-2.82931	-18.9677	Comp.	11	1.4	18.96774
	0	0	Zero	12	1.68	0
	-6.05943	-37.9472	Comp.	13	1.96	37.94724
	0	0	Zero	14	2.24	0
	-6.05943	-37.9472	Comp.	15	2.52	37.94724
	0	0	Zero	16	2.8	0
	-52.6074	-331.922	Comp.	17	3.265	331.9217
	173.8615	27.48048	Tension	18	3.265	173.8615
	-12.9315	-82.4422	Comp.	19	3.586	82.44217
10.14819	1.439439	Tension	20	3.586	10.14819	

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44.72531	6.759223	Tension	21	3.96	44.72531
-2.84875	-18.9937	Comp.	32	1.4	18.99366
0	0	Zero	33	1.68	0
-6.05943	-37.9472	Comp.	34	1.96	37.94724
0	0	Zero	35	2.24	0
-6.05943	-37.9472	Comp.	36	2.52	37.94724
-52.5318	-331.821	Comp.	37	3.265	331.8209
173.7895	27.42648	Tension	38	3.265	173.7895
-12.887	-82.3829	Comp.	39	3.586	82.38289
10.10211	1.404879	Tension	40	3.586	10.10211
44.76611	6.789823	Tension	41	3.96	44.76611

## Design of members

### *Zero members*

A36 ( $F_y = 248 \text{ MPa}$ ,  $F_u = 400 \text{ MPa}$ )

We will use L50x50x6

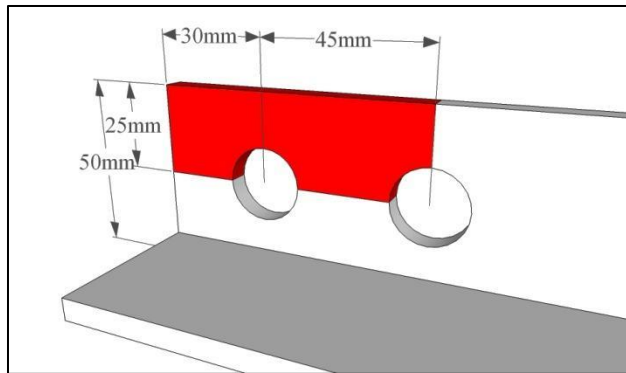
( $A = 569 \text{ mm}^2$ ,  $\bar{x} = \bar{y} = 14.5 \text{ mm}$ ,  $r_z = 9.7 \text{ mm}$ ,  $r_x = r_y = 15 \text{ mm}$ )

a) Gross section yielding for angle

$$\begin{aligned}\Phi P_n &= 0.9 A_g F_y \\ &= 0.9 * 569 * 248 * 10^{-3} \\ &= \underline{127 \text{ kN}}\end{aligned}$$

b) Tensile rupture strength for angle

$$\begin{aligned}\Phi P_n &= 0.75 A_e F_u \\ A_n &= 569 - 6(16+4) = 449 \text{ mm}^2 \\ \text{Minimum edge distance equal } (1.5 \sim 2) d \\ & (24 \text{ mm} \sim 32 \text{ mm}) \text{ take it } 30 \text{ mm} \\ \text{Center to center distance equal } (2 \frac{2}{3} \sim 3) d \\ & (43 \text{ mm} \sim 48 \text{ mm}) \text{ take it } 45 \text{ mm} \\ U &= 1 - \frac{\bar{x}}{L} = 1 - \frac{14.5}{45} = 0.678 \leftarrow \\ U &= 0.6 \text{ AISC-05 table D3-1 case 8} \\ A_e &= U A_n = 0.678 * 449 = 304.32 \text{ mm}^2 \\ \Phi P_n &= 0.75 * 304.32 * 400 * 10^{-3} = \underline{91.32 \text{ kN}}\end{aligned}$$



c) Block shear strength

$$\begin{aligned}R_n &= 0.6 A_{nv} F_u + U_s A_{nt} F_u \leq 0.6 A_{gv} F_y + U_s \\ & A_{nt} F_u \\ A_{gv} &= 6 * (45+30) = 450 \text{ mm}^2, A_{nv} = 450 - 1.5 * 6 * 20 = 270 \text{ mm}^2, A_{nt} = 6(25 - 0.5 * 20) = 90 \text{ mm}^2 \\ R_n &= 10^{-3} (0.6 * 270 * 400 + 1.0 * 90 * 400) \leq 10^{-3} (0.6 * 450 * 248 + 1.0 * 90 * 400) \\ &= 100.8 < 102.96 \\ \Phi R_n &= 0.75 * R_n = \underline{75.6 \text{ kN}}\end{aligned}$$

d) slenderness ratio

$$\frac{Kl}{r} = \frac{2800}{9.7} = 288.66 < 300 \text{ OK}$$

e) Bearing strength of bolts

$$\begin{aligned}R_{n \text{ of 1bolt}} &= 1.2 L_c t F_u \leq 2.4 d t F_u \\ L_c &= 30 - 0.5 * 20 = \underline{20 \text{ mm}} \text{ or } L_c = 45 - 1 * 20 = 25 \text{ mm} \\ R_n &= 2(1.2 * 20 * 6 * 400) * 10^{-3} \leq 2 * 10^{-3} (2.4 * 16 * 6 * 400) \\ &= 115.2 < 184.32 \\ \Phi R_n &= 0.75 R_n = \underline{86.4 \text{ kN}}\end{aligned}$$



f) Shearing strength of bolts

$$R_{n \text{ of 1bolt}} = F_{nv} A_b = 2(330 * \frac{\pi 16^2}{4}) * 10^{-3} = 132.7 \text{ kN}$$

$$\Phi R_n = 0.75 * R_n = \underline{99.526 \text{ kN}}$$

*∴ Use L50x50x6 for members No. (12 , 14 , 16 , 33 , 35 )*

---

**Checking compression strength of L50x50x6 with 1.96m length**

$$\frac{L}{r_x} = \frac{1960}{15} = 130.66 > 80$$

$$\therefore \frac{Kl}{r_z} = 32 + 1.25 \frac{L}{r_x} \leq 200 \rightarrow \frac{Kl}{r_z} = 32 + 1.25 * 130.66 = 195.325$$

$$, 4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$\frac{Kl}{r_z} > 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = 0.877 F_e$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{195.325^2} = 51.735 \text{ MPa} \rightarrow F_{cr} = 0.877 * 51.735 = 45.372 \text{ MPa}$$

$$P_n = A_g F_{cr} = 569 * 45.372 * 10^{-3} = 25.81 \text{ kN}$$

$$\Phi P_n = 0.9 P_n = 23.235 \text{ kN}$$

*∴ Use L50x50x6 for members No. (11 , 32)*

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**For members 20 , 40**

$$r_{reqd} = \frac{3586}{300} = 11.953 \text{ mm}$$

*∴ Use L65x65x7 for members No. (20 , 40)*

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**For members 21, 41**

$$r_{reqd} = \frac{3960}{300} = 13.2 \text{ mm}$$

*∴ Use L70x70x6 for members No. (21 , 41)*

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**For members 18, 38**

$$P_u = 173.8615 \text{ kN}$$

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$$1) \text{ Min } A_g = \frac{p_u}{\phi F_y} = \frac{173.86 \times 10^3}{0.9 \times 248} = 779 \text{ mm}^2$$

2) Assume  $U=0.85$

$$\text{Min } A_{g \text{ reqd}} = \frac{p_u}{\phi F_u U} + \text{area of bolts hole} =$$

$$\frac{173.86 \times 10^3}{0.75 \times 400 \times 0.85} + (16 + 4)t$$

$$= 682 + 20t$$

$$3) \text{ Min } r_{\text{reqd}} = \frac{3265}{300}$$

$$= 10.88 \text{ mm}$$

Try L60x60x8 ( $A=903 \text{ mm}^2$ ,  $\bar{x}=\bar{y}=17.7 \text{ mm}$ ,  $r_z=11.6 \text{ mm}$ ,  $r_x=r_y=18.0 \text{ mm}$ )

a) Bearing strength of bolts

$$R_{n \text{ of 1bolt}} = 1.2 L_c t F_u \leq 2.4 d t F_u$$

$$L_c = 35 - 0.5 \times 20 = 25 \text{ mm or } L_c = 45 - 1 \times 20 = 25 \text{ mm}$$

$$R_n = 3(1.2 \times 25 \times 8 \times 400) \times 10^{-3} \leq 2 \times 10^{-3} (2.4 \times 16 \times 8 \times 400)$$

$$= 288 < 368.64$$

$$\phi R_n = 0.75 R_n = \underline{218 \text{ kN}} \quad \text{OK}$$

b) Shearing strength of bolts

$$R_{n \text{ of 1bolt}} = F_{nv} A_b = 3(414 \times \frac{\pi 16^2}{4}) \times 10^{-3} = 249.72 \text{ kN}$$

$$\phi R_n = 0.75 \times R_n = \underline{187.29 \text{ kN}} \text{ (A325M threads are excluded from shear plane)}$$

c) Block shear strength

$$R_n = 0.6 A_{nv} F_u + U_s A_{nt} F_u \leq 0.6 A_{gv} F_y + U_s A_{nt} F_u$$

$$A_{gv} = 8 \times (2 \times 45 + 35) = 1000 \text{ mm}^2, A_{nv} = 1000 - 2.5 \times 8 \times 20 = 600 \text{ mm}^2, A_{nt} = 6(30 - 0.5 \times 20) = 160 \text{ mm}^2$$

$$R_n = 10^{-3} (0.6 \times 600 \times 400 + 1.0 \times 160 \times 400) \leq 10^{-3} (0.6 \times 1000 \times 248 + 1.0 \times 160 \times 400)$$

$$= 208 < 212.8$$

$$\phi R_n = 0.75 \times R_n = \underline{156 \text{ kN}} < P_u \text{ (Not OK try with 4 bolts)}$$

$$A_{gv} = 8 \times (3 \times 45 + 35) = 1360 \text{ mm}^2, A_{nv} = 1360 - 3.5 \times 8 \times 20 = 800 \text{ mm}^2, A_{nt} = 6(30 - 0.5 \times 20) = 160 \text{ mm}^2$$

$$R_n = 10^{-3} (0.6 \times 800 \times 400 + 1.0 \times 160 \times 400) \leq 10^{-3} (0.6 \times 1360 \times 248 + 1.0 \times 160 \times 400)$$

$$= 250 < 266.4$$

$$\phi R_n = 0.75 \times R_n = \underline{192 \text{ kN}} \text{ OK}$$

(Note)

No need to recalculate shearing and bearing strength of bolts because it should be safe.

d) Gross section yielding of angle

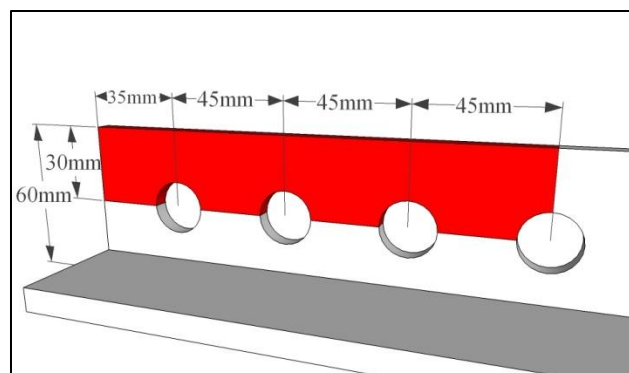
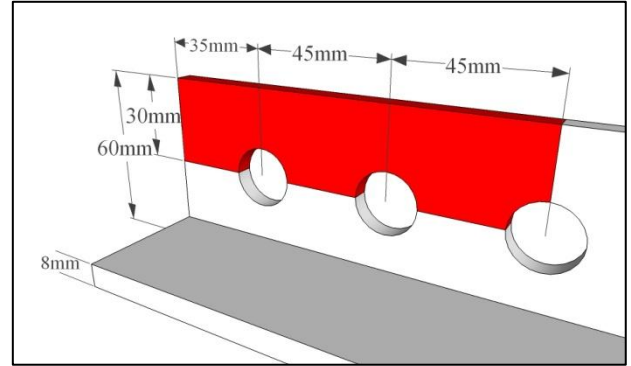
$$\phi P_n = 0.9 A_g F_y$$

$$= 0.9 \times 903 \times 248 \times 10^{-3}$$

$$= \underline{201.5 \text{ kN}} \text{ OK}$$

e) tensile rupture strength of angle

$$A_n = 903 - 8(16+4) = 743 \text{ mm}^2$$



$$U = 1 - \frac{\bar{x}}{L} = 1 - \frac{17.7}{3 \times 45} = 0.869 \leftarrow$$

$$U = 0.8 \text{ AISC-05 table D3-1 case 8}$$

$$A_e = UA_n = 0.869 \times 743 = 645.7 \text{ mm}^2$$

$$\Phi P_n = 0.75 \times 645.7 \times 400 \times 10^{-3} = \underline{193.7 \text{ kN}} \text{ OK}$$

*∴ Use L60x60x8 for members No. (18 , 38)*

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## Design of compression web members

*For members 13 , 34*

$$P_u = 37.9472 \text{ kN}$$

$$\text{Assume } \frac{Kl}{r} = 130 \text{ (near from member 11)}$$

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$\frac{Kl}{r_z} < 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = \left(0.658 \frac{F_y}{F_e}\right) F_y$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 \times 200000}{130^2} = 116.8 \text{ MPa} \rightarrow F_{cr} = \left(0.658 \frac{248}{116.8}\right) 248 = 101.97 \text{ MPa}$$

$$P_u = F_{cr} A_g \rightarrow A_g = \frac{P_u}{\phi F_{cr}} = \frac{37.9472 \times 10^3}{0.9 \times 101.97} = 413.47 \text{ mm}^2$$

Try L60x60x5 (A=582mm<sup>2</sup>, r<sub>z</sub>=11.7mm, r<sub>x</sub>=r<sub>y</sub>=18.2mm)

$$\frac{L}{r_x} = \frac{1960}{18.2} = 107.69 > 80$$

$$\therefore \frac{Kl}{r_z} = 32 + 1.25 \frac{L}{r_x} \leq 200 \rightarrow \frac{Kl}{r_z} = 32 + 1.25 \times 107.69 = 166.615 < 200$$

$$, 4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$\frac{Kl}{r_z} > 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = 0.877 F_e$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 \times 200000}{166.615^2} = 71.10 \text{ MPa} \rightarrow F_{cr} = 0.877 \times 71.10 = 62.359 \text{ MPa}$$

$$P_n = A_g F_{cr} = 582 \times 62.359 \times 10^{-3} = 36.293 \text{ kN}$$

$$\Phi P_n = 0.9 P_n = 32.66 \text{ kN not OK try larger section}$$

Try L60x60x6 (A=691mm<sup>2</sup>, r<sub>z</sub>=11.7mm, r<sub>x</sub>=r<sub>y</sub>=18.2mm)

$$\Phi P_n = 0.9 \times 691 \times 62.359 \times 10^{-3} = 38.78 \text{ kN} > P_u$$

*∴ Use L60x60x6 for members No. (13 , 34)*

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*For members 15 , 36*

We can begin with L65x65x7 (A=870mm<sup>2</sup>, r<sub>z</sub>=12.6mm, r<sub>x</sub>=r<sub>y</sub>=19.6mm)

$$\frac{L}{r_x} = \frac{2520}{19.6} = 128.571 > 80$$

$$\therefore \frac{Kl}{r_z} = 32 + 1.25 \frac{L}{r_x} \leq 200 \rightarrow \frac{Kl}{r_z} = 32 + 1.25 \times 128.571 = 192.71 < 200$$

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$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$\frac{Kl}{r_z} > 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = 0.877F_e$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{128.571^2} = 53.1498 \text{ MPa} \rightarrow F_{cr} = 0.877 * 53.1498 = 46.612 \text{ MPa}$$

$$\Phi P_n = 0.9 * 813 * 46.61 * 10^{-3} = 36.5 \text{ kN} < P_u \text{ not OK try larger section}$$

Try L70x70x6 (A=813mm<sup>2</sup>, r<sub>z</sub>=13.7mm, r<sub>x</sub>=r<sub>y</sub>=21.3mm)

$$\frac{L}{r_x} = \frac{2520}{21.3} = 118.31 > 80$$

$$\therefore \frac{Kl}{r_z} = 32 + 1.25 \frac{L}{r_x} \leq 200 \rightarrow \frac{Kl}{r_z} = 32 + 1.25 * 118.31 = 179.887 < 200$$

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$\frac{Kl}{r_z} > 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = 0.877F_e$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{179.887^2} = 60.9999 \text{ MPa} \rightarrow F_{cr} = 0.877 * 60.9999 = 53.497 \text{ MPa}$$

$$\Phi P_n = 0.9 * 813 * 53.497 * 10^{-3} = 39.14 \text{ kN} > P_u \text{ OK}$$

*∴ Use L70x70x6 for members No. (15 , 36)*

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*for members 19 , 39*

$$P_u = 82.4422 \text{ kN}$$

$$\text{Assume } \frac{Kl}{r} = 134$$

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{134^2} = 109.93 \text{ MPa} \rightarrow F_{cr} = 0.877 * 109.93 = 96.409 \text{ MPa}$$

$$P_u = F_{cr} A_g \rightarrow A_g = \frac{P_u}{F_{cr}} = \frac{82.4422 * 10^3}{0.9 * 96.409} = 950.1 \text{ mm}^2$$

Try L75x75x8 (A=1140mm<sup>2</sup>, r<sub>z</sub>=14.5mm, r<sub>x</sub>=r<sub>y</sub>=22.7mm)

$$\frac{L}{r_x} = \frac{3586}{22.7} = 157.974 > 80$$

$$\therefore \frac{Kl}{r_z} = 32 + 1.25 \frac{L}{r_x} \leq 200 \rightarrow \frac{Kl}{r_z} = 32 + 1.25 * 157.974 = 229.5 > 200 \text{ not OK try larger section}$$

Finding minimum r<sub>x</sub> from  $\frac{Kl}{r_z} = 32 + 1.25 \frac{L}{r_x} \leq 200$

$$\frac{1}{r_x} = \frac{1}{1.25 L} \times (200 - 32) \rightarrow r_{x \text{ min.}} = \frac{1.25 L}{168} = 26.68 \text{ mm}$$

Try L90x90x7 (A=1220mm<sup>2</sup>, r<sub>x</sub>=r<sub>y</sub>=27.5mm)

$$\frac{L}{r_x} = \frac{3586}{27.5} = 130.4 > 80$$

$$\therefore \frac{Kl}{r_z} = 32 + 1.25 \frac{L}{r_x} \leq 200 \rightarrow \frac{Kl}{r_z} = 32 + 1.25 * 130.4 = 195 < 200$$

$$\frac{Kl}{r_z} > 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = 0.877F_e$$

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$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{195^2} = 51.911 \text{ MPa} \rightarrow F_{cr} = 0.877 * 51.911 = 45.526 \text{ MPa}$$

$$\Phi P_n = 0.9 * 1220 * 45.526 * 10^{-3} = 49.99 \text{ kN} < P_u \text{ not OK try larger section}$$

Try L100x100x8 (A=1550mm<sup>2</sup>, r<sub>x</sub>=r<sub>y</sub>=30.6mm)

$$\frac{L}{r_x} = \frac{3586}{30.6} = 117.1895 > 80$$

$$\therefore \frac{Kl}{r_z} = 32 + 1.25 \frac{L}{r_x} \leq 200 \rightarrow \frac{Kl}{r_z} = 32 + 1.25 * 117.1895 = 178.487 < 200$$

$$\frac{Kl}{r_z} > 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = 0.877 F_e$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{178.487^2} = 61.961 \text{ MPa} \rightarrow F_{cr} = 0.877 * 61.961 = 54.34 \text{ MPa}$$

$$\Phi P_n = 0.9 * 1550 * 54.34 * 10^{-3} = 75.8 \text{ kN} < P_u \text{ not OK try larger section}$$

Try L100x100x10 (A=1920mm<sup>2</sup>, r<sub>x</sub>=r<sub>y</sub>=30.4mm)

$$\frac{L}{r_x} = \frac{3586}{30.4} = 117.96 > 80$$

$$\therefore \frac{Kl}{r_z} = 32 + 1.25 \frac{L}{r_x} \leq 200 \rightarrow \frac{Kl}{r_z} = 32 + 1.25 * 117.96 = 179.45 < 200$$

$$\frac{Kl}{r_z} > 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = 0.877 F_e$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{179.45^2} = 61.297 \text{ MPa} \rightarrow F_{cr} = 0.877 * 61.297 = 53.758 \text{ MPa}$$

$$\Phi P_n = 0.9 * 1920 * 53.758 * 10^{-3} = 92.89 \text{ kN} > P_u \text{ OK}$$

*∴ Use L100x100x10 for members No. (19, 39)*

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**For members 17, 37**

$$P_u = 331.821 \text{ kN}$$

$$\text{Assume } \frac{Kl}{r} = 100 < 4.71 \sqrt{\frac{E}{F_y}}$$

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{100^2} = 197.39 \text{ MPa} \rightarrow F_{cr} = \left(0.658 \frac{F_y}{F_e}\right) F_y$$

$$F_{cr} = \left(0.658 \frac{248}{133.755}\right) 248 = 146.58 \text{ MPa}$$

$$P_u = F_{cr} A_g \rightarrow A_g = \frac{P_u}{\phi F_{cr}} = \frac{331.821 * 10^3}{0.9 * 146.58} = 2515.3 \text{ mm}^2$$

Try L120x120x11 (A=2540mm<sup>2</sup>, r<sub>z</sub>=23.5mm, r<sub>x</sub>=r<sub>y</sub>=36.3mm)

$$\frac{L}{r_x} = \frac{3265}{36.3} = 89.945 > 80$$

$$\therefore \frac{Kl}{r_z} = 32 + 1.25 \frac{L}{r_x} \leq 200 \rightarrow \frac{Kl}{r_z} = 32 + 1.25 * 89.945 = 144.43 < 200$$

$$\frac{Kl}{r_z} > 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = 0.877 F_e$$

## (ROOF TRUSS) Structural Steel Project

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{144.43^2} = 94.625 \text{ MPa} \rightarrow F_{cr} = 0.877 * 94.625 = 82.987 \text{ MPa}$$

$$\Phi P_n = 0.9 * 2540 * 94.625 * 10^{-3} = 189.707 \text{ kN} < P_u \text{ not OK try larger section}$$

Try L140x140x10 (A=2720mm<sup>2</sup>, r<sub>z</sub>=27.6mm, r<sub>x</sub>=r<sub>y</sub>=43mm)

$$\frac{L}{r_x} = \frac{3265}{43} = 75.93 < 80$$

$$\frac{Kl}{r_z} = 72 + 0.75 * 75.93 = 128.948$$

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{128.948^2} = 118.714 \text{ MPa} \rightarrow F_{cr} = \left(0.658 \frac{F_y}{F_e}\right) F_y$$

$$F_{cr} = \left(0.658 \frac{248}{118.714}\right) 248 = 103.45 \text{ MPa}$$

$$\Phi P_n = 0.9 * 2720 * 103.45 * 10^{-3} = 253.24 \text{ kN} < P_u \text{ not OK try larger section}$$

Try L150x150x10 (A=2930mm<sup>2</sup>, r<sub>z</sub>=29.6mm, r<sub>x</sub>=r<sub>y</sub>=46.2mm)

$$\frac{L}{r_x} = \frac{3265}{46.2} = 70.671 < 80$$

$$\frac{Kl}{r_z} = 72 + 0.75 * 70.671 = 125.003$$

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{125.003^2} = 126.324 \text{ MPa} \rightarrow F_{cr} = \left(0.658 \frac{F_y}{F_e}\right) F_y$$

$$F_{cr} = \left(0.658 \frac{248}{126.324}\right) 248 = 109.042 \text{ MPa}$$

$$\Phi P_n = 0.9 * 2930 * 109.042 * 10^{-3} = 287.54 \text{ kN} < P_u \text{ not OK try larger section}$$

Try L150x150x12 (A=3480mm<sup>2</sup>, r<sub>x</sub>=r<sub>y</sub>=46.0mm)

$$\frac{L}{r_x} = \frac{3265}{46.0} = 79.783 < 80$$

$$\frac{Kl}{r_z} = 72 + 0.75 * 79.783 = 125.234$$

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{125.234^2} = 125.8599 \text{ MPa} \rightarrow F_{cr} = \left(0.658 \frac{F_y}{F_e}\right) F_y$$

$$F_{cr} = \left(0.658 \frac{248}{125.8599}\right) 248 = 108.7116 \text{ MPa}$$

$$\Phi P_n = 0.9 * 3480 * 108.7116 * 10^{-3} = 340.485 \text{ kN}$$

**∴ Use L150x150x12 for members No. (17, 37)**

## Design of Chord members

*Design of lower chord*

**For members 1, 2, 3, 4, 22, 23, 24, 25**

$$P_u = 498.3 \text{ kN}$$

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Designing 2Ls back to back with 10mm thickness of slices between the angles

$$1) \min A_{g \text{ reqd}} = \frac{P_u}{\phi F_y} = \frac{498.3 \times 10^3}{0.9 \times 248} = 2232.5 \text{ mm}^2$$

$$2) \min A_{g \text{ reqd}} = \frac{P_u}{\phi F_u U} + \text{estimated holes of area} = \frac{498.3 \times 10^3}{0.75 \times 400 \times 0.85} + 2(16+4)t = 1954.1 + 40t$$

$$3) \min r = \frac{L}{300} = \frac{2800}{300} = 9.33 \text{ mm}$$

Try 2Ls 75x75x8 (A=1140mm<sup>2</sup>, r<sub>x</sub>=r<sub>y</sub>= 22.7mm,

l<sub>x</sub>=l<sub>y</sub>=588700mm<sup>4</sup>,  $\bar{x} = \bar{y} = 21.3\text{mm}$ )

Total area = 2\*1140 = 2280 mm<sup>2</sup>

l<sub>x</sub> = 2\*588700 = 1177000 mm<sup>4</sup>, l<sub>y</sub> =

2(588700+2\*1140\*(5+21.3)<sup>2</sup>) = 4331506.4 mm<sup>4</sup>

$$r_{\min} = r_y = \sqrt{\frac{I_y}{A}} = \sqrt{\frac{4331506.4}{2280}} = 43.587 \text{ mm}$$

a) Gross section yielding

$$\phi P_n = 0.9 \times 2280 \times 248 \times 10^{-3} = 508.9 \text{ kN} > P_u \text{ OK}$$

b) Tensile rupture strength

$$A_n = 2280 - 2(16+4) \times 8 = 2200 \text{ mm}^2$$

$$U = 1 - \frac{\bar{x}}{L} = 1 - \frac{21.3}{3 \times 45} = 0.8422 \text{ or } U = 0.6 \text{ table D-3.1 AISC Manual}$$

$$A_e = 0.8422 \times 2200 = 1852.89 \text{ mm}^2$$

$$\phi P_n = 0.75 \times 1852.89 \times 400 \times 10^{-3} = 555.87 \text{ kN} > P_u \text{ OK}$$

c) Slenderness ratio

$$\frac{K_l}{r} = \frac{2800}{43.587} = 64.239 < 300 \text{ OK}$$

Check if tie plate is required  $r_{\min} = \frac{2800}{300} = 9.333 \text{ mm}$ ,  $r_z = 14.5 \text{ mm} > r_{\min} \rightarrow$  no need for tie plate

d) Bearing strength of bolts

$$R_n \text{ of one bolt} = 1.2 L_c t F_u \leq 2.4 d t F_u$$

$$L_c = 45 - 1 \times 20 = 25 \text{ mm}$$

$$R_n = (1.2 \times 25 \times 8 \times 400) \times 10^{-3} \leq 10^{-3} (2.4 \times 16 \times 8 \times 400) = 96 < 122.88$$

$$\text{No. of bolts reqd.} = \frac{P_u}{\phi R_n} = \frac{498.3}{0.75 \times 96} = 6.92 \text{ say } 7 \text{ bolts}$$

c) Shearing strength of bolts

$$R_n = m F_{nv} A_b = 2 \left( 330 \times \frac{\pi 16^2}{4} \right) \times 10^{-3} = 132.7 \text{ kN}$$

$$\text{No. of bolts reqd.} = \frac{498.3}{0.75 \times 132.7} = 5.006 \text{ say } 6 \text{ bolts}$$

Due to 7 bolts are required we will put them in two lines with change in the section

Try L100x75x8 (A=1336mm<sup>2</sup>, r<sub>x</sub>= 31.8mm<sup>4</sup>, r<sub>y</sub>= 22.2mm, l<sub>x</sub>= 1348673mm<sup>4</sup>, l<sub>y</sub>=656123 mm<sup>4</sup>,

$\bar{x} = 19.0\text{mm}$ ,  $\bar{y} = 31.5\text{mm}$ )

d) gross section yielding

$$\phi P_n = 0.9 \times (2 \times 1336) \times 248 \times 10^{-3} = 596.39 \text{ kN} > P_u \text{ OK}$$

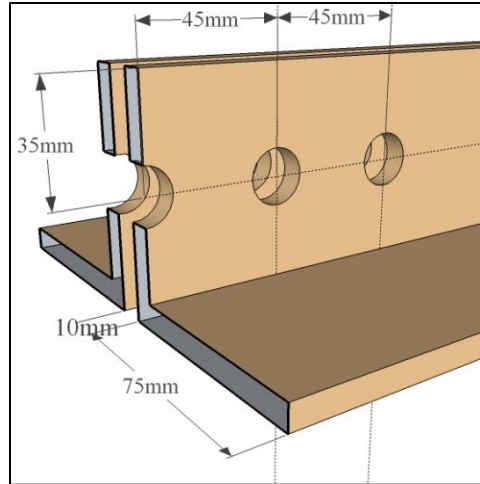
e) Tensile rupture strength

$$A_n = (2 \times 1336) - 4 \times (16+4) \times 8 = 2032 \text{ mm}^2$$

$$U = 1 - \frac{\bar{x}}{L} = 1 - \frac{31.5}{3 \times 45} = 0.767 \text{ or } U = 0.6 \text{ table D-3.1 AISC Manual}$$

$$A_e = 0.767 \times 2032 = 1558.544 \text{ mm}^2$$

$$\phi P_n = 0.75 \times 1558.544 \times 400 \times 10^{-3} = 467.563 \text{ kN} < P_u \text{ not OK try larger section}$$



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Try 2Ls120x80x8 ( $A=1550\text{mm}^2$ ,  $r_x=38.2\text{mm}$ ,  $r_y=22.8\text{mm}$ ,  $I_x=2257000\text{mm}^4$ ,  $I_y=807600\text{mm}^4$ ,  $\bar{x}=18.7\text{mm}$ ,  $\bar{y}=38.3\text{mm}$ )

a) Tensile strength rupture

$$A_n = (2 \cdot 1550) - 4(16+4) \cdot 8 = 2460 \text{ mm}^2$$

$$U = 1 - \frac{\bar{x}}{L} = 1 - \frac{38.3}{3 \times 45} = 0.716 \text{ or } U = 0.6 \text{ table D-3.1 AISC Manual}$$

$$A_e = 0.716 \cdot 2460 = 1762.09 \text{ mm}^2$$

$$\phi P_n = 0.75 \cdot 1762.09 \cdot 400 \cdot 10^{-3} = 528.63 \text{ kN} > P_u \text{ OK}$$

b) Block shear strength

$$A_{gv} = 4 \cdot 8(2 \cdot 45 + 25) = 3840 \text{ mm}^2$$

$$A_{nv} = 4 \cdot 8(120 - 2.5 \cdot 20) = 2240 \text{ mm}^2$$

$$A_{nt} = 2 \cdot 8(45 - 20) = 400 \text{ mm}^2$$

$$R_n = 0.6 A_{nv} F_u + U_{bs} A_{nt} F_u \leq 0.6 A_{gv} F_y + U_s A_{nt} F_u$$

$$= 0.6 \cdot 2240 \cdot 400 \cdot 10^{-3} + 1.0 \cdot 400 \cdot 400 \cdot 10^{-3} \leq 0.6 \cdot 3840 \cdot 248 \cdot 10^{-3} + 1.0 \cdot 400 \cdot 400 \cdot 10^{-3}$$
$$= 697.6 < 731.392$$

$$\phi R_n = 0.75 \cdot 697.6 = 523.3 \text{ kN} > P_u \text{ OK}$$

c) Bearing strength of bolts

$$R_n = 1.2 L_c t F_u \leq 2.4 d t F_u = 6 \cdot 1.2 \cdot 25 \cdot 2 \cdot 8 \cdot 400 \cdot 10^{-3} \leq 6 \cdot 2.4 \cdot 16 \cdot 2 \cdot 8 \cdot 400 \cdot 10^{-3} = 1152 < 1474.6$$

$$\phi R_n = 864 \text{ kN} > P_u \text{ OK}$$

d) Shearing strength of bolts

$$R_n = m F_{nv} A_b = 6 \cdot 2 \left( 330 \cdot \frac{\pi 16^2}{4} \right) \cdot 10^{-3} = 796.205 \text{ kN}$$

$$\phi R_n = 0.75 \cdot 796.205 = 597.15 \text{ kN} > P_u \text{ OK}$$

*∴ Use 2Ls 120x80x8 for members No. (1, 2, 3, 4, 22, 23, 24, 25)*

**For members 5, 26**

$$P_u = 474.491 \text{ kN}$$

Try 2Ls 100x75 8 ( $A=1336\text{mm}^2$ ,  $r_z=16.2$ ,  $\bar{x}=19.0$ ,  $\bar{y}=31.5\text{mm}$ )

a) Gross section yielding

$$\phi P_n = 0.9 \cdot (2 \cdot 1336) \cdot 248 \cdot 10^{-3} = 596.39 \text{ kN} > P_u \text{ OK}$$

b) Tensile rupture strength

$$A_n = 2 \cdot 1336 - 4 \cdot 8 \cdot (16+4) = 2032 \text{ mm}^2$$

$$U = 1 - \frac{\bar{x}}{L} = 1 - \frac{31.5}{2 \cdot 45} = 0.65 \leftarrow, U = 0.6 \text{ AISC-05 table D3-1 case 8}$$

$$A_e = U A_n = 0.65 \cdot 2032 = 1320.8 \text{ mm}^2$$

$$\phi P_n = 0.75 \cdot 1320.8 \cdot 400 \cdot 10^{-3} =$$

$$396.24 < P_u \text{ try with larger section}$$

Try 2Ls 100x75x10 ( $A=1650\text{mm}^2$ ,

$\bar{x}=19.8$ ,  $\bar{y}=32.3\text{mm}$ )

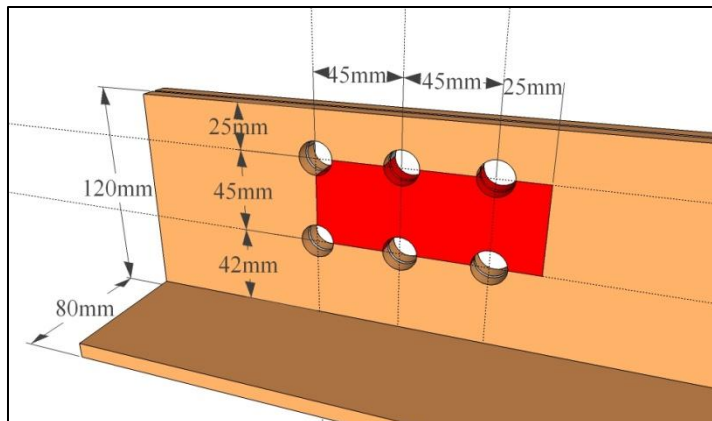
$$A_n = 2 \cdot 1650 - 4 \cdot 10 \cdot (16+4) = 2500 \text{ mm}^2$$

$$U = 1 - \frac{\bar{x}}{L} = 1 - \frac{32.3}{2 \cdot 45} = 0.6422 \leftarrow, U =$$

0.6 AISC-05 table D3-1 case 8

$$A_e = U A_n = 0.6422 \cdot 2500 =$$

$$1605.56 \text{ mm}^2$$





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$$\phi P_n = 0.75 * 1605.56 * 400 * 10^{-3} = 481.67 > P_u \text{ OK}$$

(Note)

Block shear, shearing strength of bolts and bearing strength of bolts are adequate comparing with previous section.

*∴ Use 2Ls 100x75x10 for members No. (5, 26)*

*Design of the upper chord members*

$$P_u = 508.6 \text{ kN}, L = 2.814 \text{ m}$$

$$\text{Assume } \frac{Kl}{r} = 50 < 4.71 \sqrt{\frac{E}{F_y}}$$

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{50^2} = 789.568 \text{ MPa} \rightarrow F_{cr} = \left(0.658^{\frac{F_y}{F_e}}\right) F_y$$

$$F_{cr} = \left(0.658^{\frac{248}{789.568}}\right) 248 = 217.45 \text{ MPa}$$

$$P_u = F_{cr} A_g \rightarrow A_g = \frac{P_u}{F_{cr}} = \frac{508.6 * 10^3}{0.9 * 217.45} = 2599 \text{ mm}^2$$

Try 2Ls100x75x8 BBLL for each angle ( $A=1336 \text{ mm}^2$ ,  $r_z=16.2 \text{ mm}$ ,  $r_x=31.8 \text{ mm}$ ,  $r_y=22.2 \text{ mm}$ ,  $I_x=1348673 \text{ mm}^4$ ,  $I_y=656123 \text{ mm}^4$ ,  $\bar{x}=19.0$ )

$$I_x = 2 * 1348673 = 2697346 \text{ mm}^4, I_y = 2(656123 + 1336(19.0+5)^2) = 2851318 \text{ mm}^4$$

$$r_y = \sqrt{\frac{I_x}{A}} = \sqrt{\frac{2697346}{2 * 1336}} = 31.77 \text{ mm}, r_y = \sqrt{\frac{I_y}{A}} = \sqrt{\frac{2851318}{2 * 1336}} = 32.67 \text{ mm}$$

$$\left(\frac{Kl}{r_x}\right) = \frac{2814}{31.77} = 88.574, \left(\frac{Kl}{r_y}\right) = \frac{2814}{32.67} = 86.134$$

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$\left(\frac{Kl}{r_x}\right) < 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = \left(0.658^{\frac{F_y}{F_e}}\right) F_y$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{88.574^2} = 251.6038 \text{ MPa}$$

$$\rightarrow F_{cr} = \left(0.658^{\frac{248}{251.6038}}\right) 248 = 164.165 \text{ MPa}$$

$$\phi P_n = 0.9 * 164.165 * (2 * 1336) * 10^{-3} = 394.78$$

$\text{kN} < P_u$  not OK try larger section

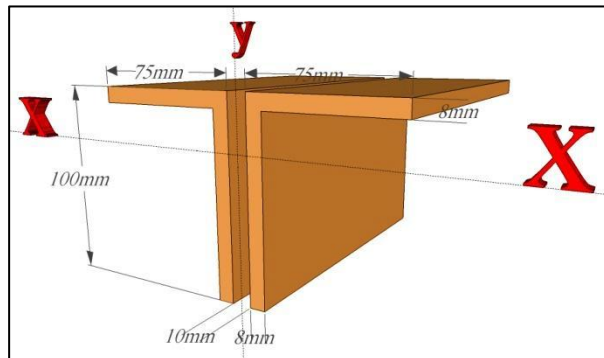
Try 2Ls120x80x8 BBLL for each angle ( $A=1550 \text{ mm}^2$ ,  $r_z=17.3 \text{ mm}$ ,  $\bar{x}=18.7$ ,  $r_x=38.2 \text{ mm}$ ,

$$r_y=22.8 \text{ mm}, I_x=2257000 \text{ mm}^4, I_y=807600 \text{ mm}^4)$$

$$I_x = 2 * 2257000 = 4514000 \text{ mm}^4, I_y = 2(807600 + 1550(18.7+5)^2) = 3356435 \text{ mm}^4$$

$$r_y = \sqrt{\frac{I_x}{A}} = \sqrt{\frac{4514000}{2 * 1550}} = 38.159 \text{ mm}, r_y = \sqrt{\frac{I_y}{A}} = \sqrt{\frac{3356435}{2 * 1550}} = 32.905 \text{ mm}$$

$$\left(\frac{Kl}{r_x}\right) = \frac{2814}{38.159} = 73.744, \left(\frac{Kl}{r_y}\right) = \frac{2814}{32.905} = 85.52$$



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$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$\left(\frac{Kl}{r_x}\right) < 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = \left(0.658 \frac{F_y}{F_e}\right) F_y$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{85.52^2} = 269.894 \text{ MPa} \rightarrow F_{cr} = \left(0.658 \frac{248}{269.894}\right) 248 = 168.82 \text{ MPa}$$

$$\phi P_n = 0.9 * 168.82 * (2 * 1550) * 10^{-3} = 471.01 \text{ kN} < P_u \text{ not OK try larger section}$$

Try 2Ls120x80x10 BBL for each angle (A=1910mm<sup>2</sup>,  $\bar{x} = 20.3$ ,  $I_x = 3228000\text{mm}^4$ ,  $I_y = 1143000\text{mm}^4$ )

$$I_x = 2 * 3228000 = 6456000 \text{ mm}^4, I_y = 2(1143000 + 1910(20.3 + 5)^2) = 4731143.8\text{mm}^4$$

$$r_y = \sqrt{\frac{I_x}{A}} = \sqrt{\frac{6456000}{2 * 1910}} = 41.11 \text{ mm}, r_y = \sqrt{\frac{I_y}{A}} = \sqrt{\frac{4731143.8}{2 * 1910}} = 35.193 \text{ mm}$$

$$\left(\frac{Kl}{r_x}\right) = \frac{2814}{41.11} = 68.45, \left(\frac{Kl}{r_y}\right) = \frac{2814}{32.905} = 79.960$$

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{200000}{248}} = 133.755$$

$$\left(\frac{Kl}{r_x}\right) < 4.71 \sqrt{\frac{E}{F_y}} \rightarrow F_{cr} = \left(0.658 \frac{F_y}{F_e}\right) F_y$$

$$F_e = \frac{\pi^2 E}{\left(\frac{Kl}{r}\right)^2} = \frac{\pi^2 * 200000}{79.960^2} = 308.7339 \text{ MPa} \rightarrow F_{cr} = \left(0.658 \frac{248}{308.7339}\right) 248 = 177.189 \text{ MPa}$$

$$\phi P_n = 0.9 * 177.189 * (2 * 1910) * 10^{-3} = 609.17 \text{ kN} > P_u \text{ OK}$$

*∴ Use 2Ls 120x80x10 for members No. (6, 7, 8, 9, 10, 27, 28, 29, 30, 31)*

*For reversal members 6, 27*

Tension force in the reversal members is too small therefore 2Ls 120x80x10 are adequate.

**Checking estimated weight of roof truss**

Here we will calculate actual internal force due to the weight of the roof truss using STAAD Pro. Then we will compare it with the internal force due to the estimated load as shown here in table 8.

Table (8)

member	Actual values		Used values	
	+ve Max Force (kN)	-ve Max Force (kN)	+ve Max Force (kN)	-ve Max Force (kN)
<b>1</b>	280.31	40.38	284.69	43.66
<b>2</b>	280.31	40.38	284.69	43.66
<b>3</b>	490.18	71.32	498.19	77.33

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4	490.18	71.32	498.19	77.33
5	466.72	67.46	474.49	73.29
6	2.05	-2.72	2.14	-2.64
7	-63.61	-429.11	-68.67	-435.86
8	-63.40	-429.11	-68.46	-435.86
9	-74.53	-500.40	-80.62	-508.52
10	-74.31	-500.40	-80.40	-508.52
11	-2.15	-18.06	-2.83	-18.97
12	1.04	0.67	0.00	0.00
13	-4.68	-36.11	-6.06	-37.95
14	1.07	0.69	0.00	0.00
15	-4.73	-36.17	-6.06	-37.95
16	1.17	0.75	0.00	0.00
17	-49.03	-327.15	-52.61	-331.92
18	171.03	25.35	173.86	27.48
19	-11.99	-81.19	-12.93	-82.44
20	9.94	1.28	10.15	1.44
21	44.17	6.34	44.73	6.76
22	280.31	38.07	284.87	41.49
23	280.31	38.07	284.87	41.49
24	490.18	70.46	498.25	76.52
25	490.18	70.46	498.25	76.52
26	466.72	67.46	474.49	73.29
27	2.05	-2.72	1.93	-2.84
28	-63.61	-429.11	-68.75	-435.97
29	-63.40	-429.11	-68.54	-435.97
30	-74.53	-500.40	-80.64	-508.55
31	-74.31	-500.40	-80.43	-508.55
32	-2.15	-18.06	-2.85	-18.99
33	1.04	0.67	0.00	0.00
34	-4.68	-36.11	-6.06	-37.95
35	1.07	0.69	0.00	0.00
36	-4.73	-36.17	-6.06	-37.95
37	-49.03	-327.15	-52.53	-331.82
38	171.03	25.35	173.79	27.43
39	-11.99	-81.19	-12.89	-82.38
40	9.94	1.28	10.10	1.40
41	44.17	6.34	44.77	6.79

The table show that our estimate of the roof truss weight is good with no problems.

## DESIGN OF THE CONNECTIONS

### Bolted connections

$L_{10}$

Member 32, compression -19 kN, L50x50x6

- a) bearing strength

$$L_c = 45 - (16 + 4) = 25 \text{ mm}$$

$$R_n = 1.2 L_c t F_u \leq 2.4 d t F_u \rightarrow 1.2 * 25 * 6 * 400 * 10^{-3} \leq 2.4 * 16 * 6 * 400 * 10^{-3} \rightarrow 72 < 92.16$$

$$\text{No. of bolts} = \frac{P_u}{\phi R_n} = \frac{19}{0.75 * 72} = 0.35 \rightarrow \text{say 2 bolts as a minimum fastener}$$

- b) shearing strength of 2 bolts

$$\phi R_n = 0.75 * F_{nv} A_b = 2 * 0.75 * 330 * \frac{\pi 16^2}{4} * 10^{-3} = 99.5 \text{ kN} > P_u \text{ OK}$$

$\therefore$  Use two bolts 16 mm in diameter.

$L_{10}$

Member 37, compression -331.8 kN, L150x150x12

- a) bearing strength of one bolt

$$L_c = 45 - (16 + 4) = 25 \text{ mm}$$

$$R_n = 1.2 L_c t F_u \leq 2.4 d t F_u \rightarrow 1.2 * 25 * 12 * 400 * 10^{-3} \leq 2.4 * 16 * 12 * 400 * 10^{-3} \rightarrow 144 < 184.32$$

$$\text{No. of bolts} = \frac{P_u}{\phi R_n} = \frac{331.8}{0.75 * 144} = 3.07 \rightarrow \text{say 4 bolts.}$$

- b) shearing strength of 4 bolts

$$\phi R_n = 0.75 * F_{nv} A_b = 4 * 0.75 * 330 * \frac{\pi 16^2}{4} * 10^{-3} = 199.05 \text{ kN} < P_u \rightarrow \text{increase the bolts.}$$

$$\text{No. of bolts reqd.} = \frac{331.8 * 10^3}{0.75 * 330 * \frac{\pi * 16^2}{4}} = 6.67 \rightarrow \text{say 7 bolts in two lines.}$$

$L_{10}$

Member 22, tension 284.9 kN, 2Ls120x80x8

- a) bearing strength of one bolt

$$L_c = 45 - (16 + 4) = 25 \text{ mm}$$

$$R_n = 1.2 L_c t F_u \leq 2.4 d t F_u \rightarrow 1.2 * 25 * 8 * 400 * 10^{-3} \leq 2.4 * 16 * 8 * 400 * 10^{-3} \rightarrow 96 < 122.88$$

$$\text{No. of bolts} = \frac{P_u}{\phi R_n} = \frac{284.9}{0.75 * 96} = 3.96 \rightarrow \text{say 4 bolts}$$

- b) shearing strength of 4 bolts

$$\phi R_n = 0.75 * F_{nv} A_b = 2 * 4 * 0.75 * 330 * \frac{\pi 16^2}{4} * 10^{-3} = 398.1 \text{ kN} > P_u$$

$\therefore$  Use four bolts 16 mm in diameter.

$U_{10}$

Member 27, reversal +1.93 kN and -2.835 kN, 2Ls120x80x10

The same with member 32

$\therefore$  Use two bolts 16 mm in diameter.

$L_9$

Member 23, tension +285 kN, 2Ls120x80x8

The same with member 22

$\therefore$  Use four bolts 16 mm in diameter.

$L_9$

Member 33, zero member 0 kN, L50x50x6

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The same with member 32

∴ Use two bolts 16 mm in diameter.

$U_9$

Member 38, tension +173.8 kN, L60x60x8

∴ Use three bolts 16 mm in diameter (page ##).

$U_9$

Member 28, comp. -436 kN, 2Ls120x80x10

a) bearing strength of one bolt

$$L_c = 45 - (16 + 4) = 25 \text{ mm}$$

$$R_n = 1.2 L_c t F_u \leq 2.4 d t F_u \rightarrow 1.2 * 25 * 10 * 400 * 10^{-3} \leq 2.4 * 16 * 10 * 400 * 10^{-3} \rightarrow 120 < 153.6$$

$$\text{No. of bolts} = \frac{P_u}{\phi R_n} = \frac{436}{0.75 * 120} = 4.84 \rightarrow \text{say 5 bolts}$$

b) shearing strength of 5 bolts

$$\phi R_n = 0.75 * F_{nv} A_b = 2 * 5 * 0.75 * 330 * \frac{\pi 16^2}{4} * 10^{-3} = 497.6 \text{ kN} > P_u \text{ OK}$$

∴ Use five bolts 16 mm in diameter.

$L_8$

Member 34, comp. -38.9 kN, L60x60x6

a) bearing strength of one bolt

$$L_c = 45 - (16 + 4) = 25 \text{ mm}$$

$$R_n = 1.2 L_c t F_u \leq 2.4 d t F_u \rightarrow 1.2 * 25 * 6 * 400 * 10^{-3} \leq 2.4 * 16 * 6 * 400 * 10^{-3} \rightarrow 72 < 92.16$$

$$\text{No. of bolts} = \frac{P_u}{\phi R_n} = \frac{38.9}{0.75 * 72} = 0.72 \rightarrow \text{use 2 bolts}$$

b) shearing strength of 2 bolts

$$\phi R_n = 99.5 \text{ kN} > P_u \text{ OK}$$

∴ Use two bolts 16 mm in diameter.

$L_8$

Member 39, comp. -82.4 kN, L100x100x10

∴ Use 2 bolts 16 mm in diameter which adequate comparing with member 34.

$U_9$

Member 24, tension +498.3 kN, 2Ls120x80x8

∴ Use 6 bolts 16 mm in diameter (page ##).

$U_8$

Member 29, comp. -436 kN, 2Ls120x80x10

a) bearing strength of one bolt

$$\text{No. of bolts} = \frac{P_u}{\phi R_n} = \frac{436}{0.75 * 120} = 4.84 \rightarrow \text{say 5 bolts}$$

b) shearing strength of 5 bolts

$$\phi R_n = 497.6 \text{ kN} > P_u \text{ OK}$$

∴ Use 5 bolts 16 mm in diameter.

$L_7$

Member 35, zero member 0 kN, L50x50x6

(ROOF TRUSS) Structural Steel Project

The same with member 32

∴ Use 2 bolts 16 mm in diameter.

$L_7$

Member 25, tension +498.3 kN, 2Ls120x80x8

∴ Use 6 bolts 16 mm in diameter (page ##).

$U_7$

Member 40, tension +10.102 kN, L65x65x7

∴ Use 2 bolts 16 mm in diameter (page ##).

$U_7$

Member 30, comp. -508.55kN, 2Ls120x80x10

a) bearing strength of one bolt

$$\text{No. of bolts} = \frac{P_u}{\phi R_n} = \frac{508.55}{0.75 \times 120} = 5.65 \rightarrow \text{say 6 bolts}$$

b) shearing strength of 6 bolts

$$\phi R_n = 0.75 * 2 * 6 * 330 * \frac{\pi 16^2}{4} * 10^{-3} = 597.1 \text{ kN} > P_u \text{ OK}$$

∴ Use 6 bolts 16 mm in diameter.

$L_6$

Member 36, comp. -37.95 kN, L65x65x7

∴ Use 2 bolts 16 mm in diameter which adequate comparing with member 34.

$L_6$

Member 41, tension 44.8 kN, L70x70x6

∴ Use 2 bolts 16 mm in diameter (page ##).

$L_6$

Member 26, tension 474.5 kN, 2Ls100x75x10

a) bearing strength of one bolt

$$\text{No. of bolts} = \frac{P_u}{\phi R_n} = \frac{474.5}{0.75 \times 120} = 5.65 \rightarrow \text{say 6 bolts}$$

b) shearing strength of 6 bolts

$$\phi R_n = 0.75 * 2 * 6 * 330 * \frac{\pi 16^2}{4} * 10^{-3} = 597.1 \text{ kN} > P_u \text{ OK}$$

∴ Use 6 bolts 16 mm in diameter.

$U_6$

Member 31, comp. -508.55 kN, 2Ls120x80x10

∴ Use 6 bolts 16 mm in diameter the same with member 30.

### Gusset plate for bolted connections

As we can see all thicknesses of the members are equal or less than 10 mm (gusset plate thickness) except member 37 has 12mm thickness but shearing strength of bolts is controls and 7 bolts are adequate. Then we will use 10 mm thickness of the gusset plate.

Table (9) summary to bolted connections

Joint	member	section	type	force	No. of bolts
L <sub>10</sub>	32	L50x50x6	comp.	-19	2
	37	L150x150x12	comp.	-331.8	7
	22	2Ls120x80x8	Tens.	285	4
U <sub>10</sub>	27	2Ls120x80x10	reversal	+1.9 -2.8	2
L <sub>9</sub>	23	2Ls120x80x8	Tens.	285	4
	33	L50x50x6	zero	0	2
U <sub>9</sub>	38	L60x60x8	Tens.	173.8	3
	28	2Ls120x80x10	comp.	436	5
L <sub>8</sub>	34	L60x60x6	comp.	-38	2
	39	L100x100x10	comp.	-82.4	2
	24	2Ls120x80x8	Tens.	498.3	6
U <sub>8</sub>	29	2Ls120x80x10	comp.	-463	5
L <sub>7</sub>	35	L50x50x6	zero	0	2
	25	2Ls120x80x8	Tens.	498.3	6
U <sub>7</sub>	40	L65x65x7	Tens.	10.102	2
	30	2Ls120x80x10	comp.	-508.3	6
L <sub>6</sub>	36	L65x65x7	comp.	-37.95	2
	41	L70x70x6	Tens.	44.8	2
	26	2Ls100x75x10	Tens.	474.5	6
U <sub>6</sub>	31	2Ls120x80x10	comp.	-508.55	6

## Welded connections

We will use 70EXX (it's strength 483MPs)

L<sub>0</sub>

Member 11, compression -19 kN, L50x50x6,  $\bar{x} = 14.5\text{mm}$

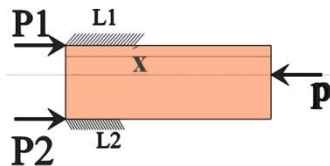
Maximum weld size = 6 mm, minimum weld size = 3mm (AISC manual table J 2.4)

Try with 4mm

$$\phi R_n = \phi F_w A_w$$

$$= 0.75 * 0.6 * 483 * (4 * 0.707) * 1 * 10^{-3} = 0.6147 \text{ kN/mm}$$

$$\text{Total length of weld required} = \frac{18.97}{0.6147} = 30.9 \text{ mm, min. length} = 4t = 4 * 6 = 24\text{mm}$$



$$\sum M_{P1} = 0 \rightarrow 18.97 * 14.4 = 50 P_2 \rightarrow P_2 = 5.5 \text{ kN} \rightarrow P_1 = 18.97 - 5.5 = 13.47 \text{ kN}$$

$$L_1 = \frac{13.47}{0.6147} = 21.9\text{mm say } 30\text{mm} \left( \frac{l}{w} = \frac{21.9}{4} = 5.475 < 100 \rightarrow \beta = 1.0 \right)$$

$$L_2 = \frac{5.5}{0.6147} = 8.9\text{mm say } 10\text{mm} \left( \frac{l}{w} = \frac{8.9}{4} = 2.225 < 100 \rightarrow \beta = 1.0 \right)$$

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$L_0$

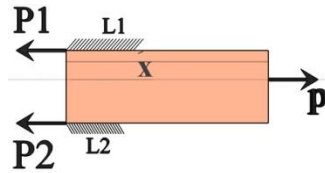
Member 1, tension +284.7 kN, 2Ls120x80x8,  $\bar{x} = 38.3\text{mm}$

Maximum weld size = (8-2) = 6 mm, minimum weld size = 5mm (AISC manual table J 2.4)

Try with 6mm

$$\phi R_n = \phi F_w A_w$$

$$= 0.75 * 0.6 * 483 * (6 * 0.707) * 1 * 10^{-3} = 0.9220 \text{ kN/mm}$$



$$\Sigma M_{P_1} = 0 \rightarrow 284.7 * 38.3 = 120 P_2 \rightarrow P_2 = 90.9 \text{ kN} \rightarrow P_1 = 284.7 - 90.9 = 193.8 \text{ kN}$$

$$L_1 = \frac{193.8}{0.922} = 210.1\text{mm say } 210\text{mm} \left( \frac{l}{w} = \frac{210}{6} = 35 < 100 \rightarrow \beta = 1.0 \right)$$

$$L_2 = \frac{90.9}{0.922} = 98.6\text{mm say } 100\text{mm} \left( \frac{l}{w} = \frac{100}{6} = 16.67 < 100 \rightarrow \beta = 1.0 \right)$$

$L_0$

Member 17, compression -331.9 kN, L150x150x12,  $\bar{x} = 41.2\text{mm}$

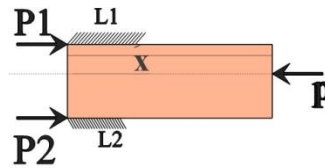
Maximum weld size = (12-2) = 10 mm, minimum weld size = 5mm (AISC manual table J 2.4)

Try with 10mm

$$\phi R_n = \phi F_w A_w$$

$$= 0.75 * 0.6 * 483 * (10 * 0.707) * 1 * 10^{-3} = 1.537 \text{ kN/mm}$$

$$\Sigma M_{P_1} = 0 \rightarrow 331.9 * 41.2 = 150 P_2 \rightarrow P_2 = 91.16 \text{ kN} \rightarrow P_1 = 331.9 - 91.16 = 240.7 \text{ kN}$$



$$L_1 = \frac{240.7}{1.537} = 156.7\text{mm say } 160\text{mm} \left( \frac{l}{w} = \frac{160}{10} = 16 < 100 \rightarrow \beta = 1.0 \right)$$

$$L_2 = \frac{91.16}{1.537} = 8.9\text{mm say } 60\text{mm} \left( \frac{l}{w} = \frac{60}{10} = 6 < 100 \rightarrow \beta = 1.0 \right)$$

$U_0$

Member 6, reversal +2.142 kN and -2.640 kN, 2Ls120x80x10,  $\bar{x} = 39.2\text{mm}$

Maximum weld size = (10-2) = 8 mm, minimum weld size = 5mm (AISC manual table J 2.4)

Try with 5mm

$$\phi R_n = \phi F_w A_w$$

$$= 0.75 * 0.6 * 483 * (5 * 0.707) * 1 * 10^{-3} = 0.7683 \text{ kN/mm}$$

$$\text{Total length of weld required} = \frac{2.64}{0.7683} = 3.4 \text{ mm, min. length} = 4t = 4 * 5 = 20\text{mm}$$

$$L_1 = 10\text{mm}, L_2 = 10\text{mm}$$

$L_1$

Member 12, zero 0 kN, L50x50x6,  $\bar{x} = 14.5\text{mm}$

Use minimum weld size, minimum weld size = 3mm (AISC manual table J 2.4)

Min. length = 4t = 4 \* 3 = 12mm

$$L_1 = 10\text{mm}, L_2 = 10\text{mm}$$



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**L<sub>1</sub>**

Member 2, tension +284.7 kN, 2Ls120x80x8,  $\bar{x} = 38.3\text{mm}$

Use  $L_1 = 10\text{mm}$ ,  $L_2 = 10\text{mm}$  the same with member 1

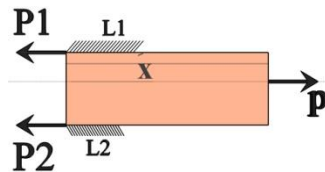
**U<sub>1</sub>**

Member 18, tension +173.9 kN, L60x60x8,  $\bar{x} = 16.9\text{mm}$

Maximum weld size = 6 mm, minimum weld size = 5mm (AISC manual table J 2.4)

Try with 6mm

$\phi R_n = 0.9220 \text{ kN/mm}$



$$\Sigma M_{P_1} = 0 \rightarrow 173.9 * 16.9 = 60 P_2 \rightarrow P_2 = 48.98 \text{ kN} \rightarrow P_1 = 173.9 - 48.98 = 124.92 \text{ kN}$$

$$L_1 = \frac{124.92}{0.922} = 135.5\text{mm say } 140\text{mm} \left( \frac{l}{w} = \frac{140}{6} = 23.33 < 100 \rightarrow \beta = 1.0 \right)$$

$$L_2 = \frac{48.98}{0.922} = 53.1\text{mm say } 60\text{mm} \left( \frac{l}{w} = \frac{60}{6} = 10 < 100 \rightarrow \beta = 1.0 \right)$$

**U<sub>1</sub>**

Member 7, compression -435.66 kN, 2Ls120x80x10,  $\bar{x} = 39.2\text{mm}$

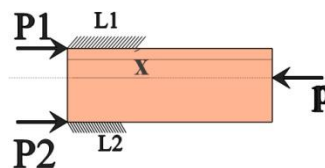
Maximum weld size =  $(10-2) = 8 \text{ mm}$ , minimum weld size = 5mm (AISC manual table J 2.4)

Try with 8mm

$\phi R_n = \phi F_w A_w$

$$= 0.75 * 0.6 * 483 * (8 * 0.707) * 1 * 10^{-3} = 1.229 \text{ kN/mm}$$

$$\Sigma M_{P_1} = 0 \rightarrow 39.2 * 435.86 = 120 P_2 \rightarrow P_2 = 142.38 \text{ kN} \rightarrow P_1 = 435.86 - 142.38 = 293.48 \text{ kN}$$



$$L_1 = \frac{293.48}{1.229} = 238.8\text{mm say } 240\text{mm} \left( \frac{l}{w} = \frac{240}{8} = 30 < 100 \rightarrow \beta = 1.0 \right)$$

$$L_2 = \frac{142.38}{1.229} = 115.9\text{mm say } 120\text{mm} \left( \frac{l}{w} = \frac{120}{8} = 15 < 100 \rightarrow \beta = 1.0 \right)$$

**L<sub>2</sub>**

Member 19, compression -82.44 kN, L100x100x10,  $\bar{x} = 39.2\text{mm}$

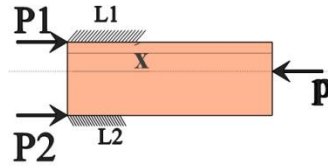
Maximum weld size =  $(10-2) = 8 \text{ mm}$ , minimum weld size = 5mm (AISC manual table J 2.4)

Try with 6mm

$\phi R_n = \phi F_w A_w = 0.9220 \text{ kN/mm}$

$$\Sigma M_{P_1} = 0 \rightarrow 82.44 * 28.2 = 100 P_2 \rightarrow P_2 = 23.25 \text{ kN} \rightarrow P_1 = 59.19 \text{ kN}$$

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$$L_1 = \frac{59.19}{0.922} = 64.2\text{mm say } 70\text{mm}, L_2 = \frac{23.25}{0.922} = 25.2\text{mm say } 30\text{mm}$$

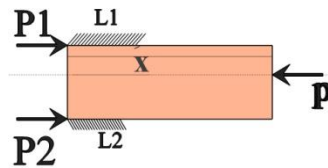
$L_2$

Member 13, compression -37.947 kN, L60x60x6,  $\bar{x} = 16.9\text{mm}$

Try with 4mm

$$\phi R_n = \phi F_w A_w = 0.6147 \text{ kN/mm}$$

$$\Sigma M_{P_1} = 0 \rightarrow 37.947 * 16.9 = 60 P_2 \rightarrow P_2 = 10.69 \text{ kN} \rightarrow P_1 = 27.26 \text{ kN}$$



$$L_1 = \frac{27.26}{0.6147} = 44.35\text{mm say } 50\text{mm}, L_2 = \frac{10.69}{0.6147} = 17.8\text{mm say } 20\text{mm}$$

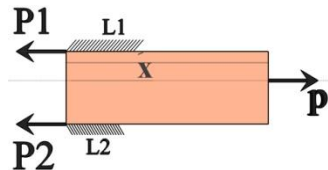
$L_2$

Member 3, tension +498.19 kN, 2Ls120x80x8,  $\bar{x} = 38.3\text{mm}$

Maximum weld size = 6 mm, minimum weld size = 5mm (AISC manual table J 2.4)

Try with 6mm

$$\phi R_n = 0.9220 \text{ kN/mm}$$



$$\Sigma M_{P_1} = 0 \rightarrow 498.19 * 38.3 = 120 P_2 \rightarrow P_2 = 159 \text{ kN} \rightarrow P_1 = 339.18 \text{ kN}$$

$$L_1 = \frac{339.18}{0.922} = 367.9\text{mm say } 370\text{mm} \left( \frac{l}{w} = \frac{370}{6} = 61.67 < 100 \rightarrow \beta = 1.0 \right)$$

$$L_2 = \frac{159}{0.922} = 172.5\text{mm say } 180\text{mm} \left( \frac{l}{w} = \frac{180}{6} = 30 < 100 \rightarrow \beta = 1.0 \right)$$

$U_2$

Member 8,  $L_1 = 120\text{mm}$ ,  $L_2 = 240\text{mm}$  the same with member 7

$L_3$

Member 4,  $L_1 = 50\text{mm}$ ,  $L_2 = 20\text{mm}$  the same with member 3

$L_3$

Member 14,  $L_1 = 10\text{mm}$ ,  $L_2 = 10\text{mm}$  the same with member 12

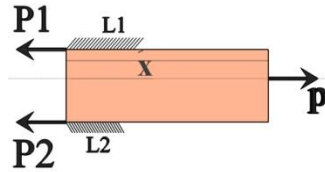
$U_3$

Member 20, tension +10.15 kN, L65x65x7,  $\bar{x} = 18.5\text{mm}$

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Using minimum weld size = 5mm (AISC manual table J 2.4)

$$\phi R_n = 0.7683 \text{ kN/mm}$$



$$\text{Total length} = \frac{10.15}{0.7683} = 13.21 \text{ mm, minimum length of weld} = 4w = 4 \cdot 5 = 20 \text{ mm} \leftarrow$$

$$\Sigma M_{P_1} = 0 \rightarrow 20 \cdot 18.5 = 65 L_2 \rightarrow L_2 = 5.7 \text{ mm say } 10 \text{ mm}$$

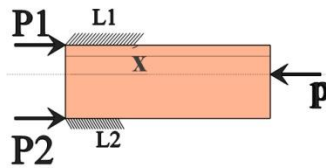
$$L_1 = 20 - 5.7 = 14.3 \text{ mm, say } 20 \text{ mm}$$

**U<sub>3</sub>**

Member 9, compression -508.5 kN, 2Ls120x80x10,  $\bar{y} = 39.2 \text{ mm}$

Use maximum weld size 10 - 2 = 8mm

$$\phi R_n = \phi F_w A_w = 1.229 \text{ kN/mm}$$



$$\Sigma M_{P_1} = 0 \rightarrow 508.5 \cdot 39.2 = 120 P_2 \rightarrow P_2 = 166.11 \text{ kN} \rightarrow P_1 = 342.39 \text{ kN}$$

$$L_1 = \frac{342.39}{1.229} = 278.6 \text{ mm say } 280 \text{ mm, } L_2 = \frac{166.11}{1.229} = 135.2 \text{ mm say } 140 \text{ mm}$$

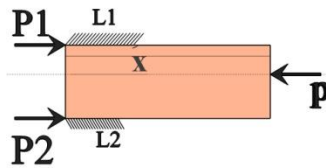
**L<sub>4</sub>**

Member 15, compression -37.95 kN, L70x70x6,  $\bar{x} = 19.3 \text{ mm}$

Try with 3mm (AISC manual table J 2.4)

$$\phi R_n = \phi F_w A_w = 0.75 \cdot 0.6 \cdot 483 \cdot 3 \cdot 0.707 \cdot 10^{-3} = 0.4610 \text{ kN/mm}$$

$$\Sigma M_{P_1} = 0 \rightarrow 37.95 \cdot 19.3 = 70 P_2 \rightarrow P_2 = 10.46 \text{ kN} \rightarrow P_1 = 27.49 \text{ kN}$$



$$L_1 = \frac{27.49}{0.4610} = 59.6 \text{ mm say } 60 \text{ mm, } L_2 = \frac{10.46}{0.4610} = 22.7 \text{ mm say } 30 \text{ mm}$$

**Note**

Members 5, 21 and 10 prefer to use bolted connection for erection purpose the same with members 26, 41, and 31 respectively.

Table (10) summary to welded connections

Joint	Member	Section	w (mm)	L <sub>1</sub> (mm)	L <sub>2</sub> (mm)
L <sub>0</sub>	11	L50x50x6	4	30	10
	1	2Ls120x80x8	6	210	100
	17	L150x150x12	10	160	60
U <sub>0</sub>	6	2Ls120x80x10	5	10	10
L <sub>1</sub>	12	L50x50x6	3	10	10
	2	2Ls120x80x8	6	210	100
U <sub>1</sub>	18	L60x60x8	6	140	60
	7	2Ls120x80x10	8	240	120
L <sub>2</sub>	19	L100x100x10	6	70	30
	13	L60x60x6	4	50	20
	3	2Ls120x80x8	6	370	180
U <sub>2</sub>	8	2Ls120x80x10	8	240	120
L <sub>3</sub>	4	2Ls120x80x8	6	370	180
	14	L50x50x6	3	10	10
U <sub>3</sub>	20	L65x65x7	5	20	10
	9	2Ls120x80x10	8	280	140
L <sub>4</sub>	15	L70x70x6	3	60	30

As we were drawing we noted that, some members can't install like members 17 and 19. Then we will recalculate their lengths as shown hear.

L<sub>0</sub>

Member 17, w = 10 mm

160mm length provide  $0.75 \cdot 0.6 \cdot 483 \cdot 10 \cdot 0.707 \cdot 160 \cdot 10^{-3} = 245.87$  kN

$$\Rightarrow P_2 = 331.9 - 245.87 = 86.03 \text{ kN}$$

The resistance provided by 1mm length in the transverse direction equal

$$= 0.75 \cdot 0.6 \cdot 483 \cdot (1.0 + 0.5 \sin^{1.5} 90^\circ) \cdot (10 \cdot 0.707) \cdot 1 \cdot 10^{-3}$$

$$= 2.305 \text{ kN/mm}$$

$$\text{Reqd. length} = \frac{86.03}{2.305} = 37.32 \text{ mm say } 40 \text{ mm}$$

Check  $R_u = R_{wl} + R_{wt}$  or  $R_u = 0.85 R_{wl} + 1.5 R_{wt}$

$$= 1.537 \cdot 160 + 2.305 \cdot 40 = 338.12 \text{ kN} > P_u \text{ OK}$$

$$= 0.85(1.537 \cdot 160) + 1.5(2.305 \cdot 40) = 347.33 \text{ kN} > P_u \text{ OK}$$

Use 40mm transverse weld

L<sub>2</sub>

Member 19

L = 70mm  $\rightarrow \phi R_n = 0.922 \cdot 70 = 64.54$  kN

The resistance provided by 1mm length in the transverse direction equal

$$= 0.75 \cdot 0.6 \cdot 483 \cdot (1.0 + 0.5 \sin^{1.5} 90^\circ) \cdot (10 \cdot 0.707) \cdot 1 \cdot 10^{-3}$$

$$= 1.383 \text{ kN/mm}$$

$$\text{Reqd. length} = \frac{82.44 - 64.54}{1.383} = 12.9 \text{ mm say } 20 \text{ mm}$$

Check  $R_u = R_{wl} + R_{wt}$  or  $R_u = 0.85 R_{wl} + 1.5 R_{wt}$

$$= 0.922 \cdot 70 + 1.383 \cdot 20 = 92.2 \text{ kN} > P_u \text{ OK}$$

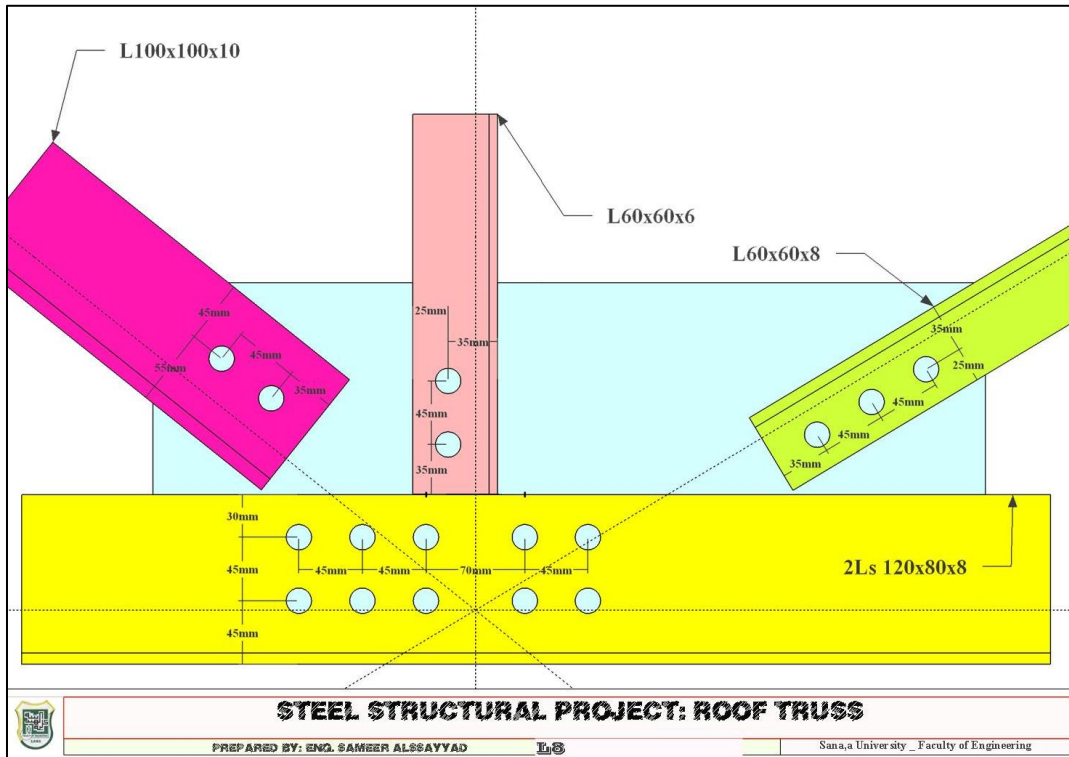
$$= 0.85(0.922*70) + 1.5(1.383*20) = 96.35\text{kN} > P_u \text{ OK}$$

Use 20mm transverse weld

### Drawing of the connections

The drawings are show in figure 17 as a sample for bolted connections, a sample for gusset plates in figure 18 and a sample for welded connections in figure 19. All the connections and their gusset plates are presented in PDF file also in JPEG and PNG format with the project.

Fig. (17) bolted connection L<sub>8</sub>



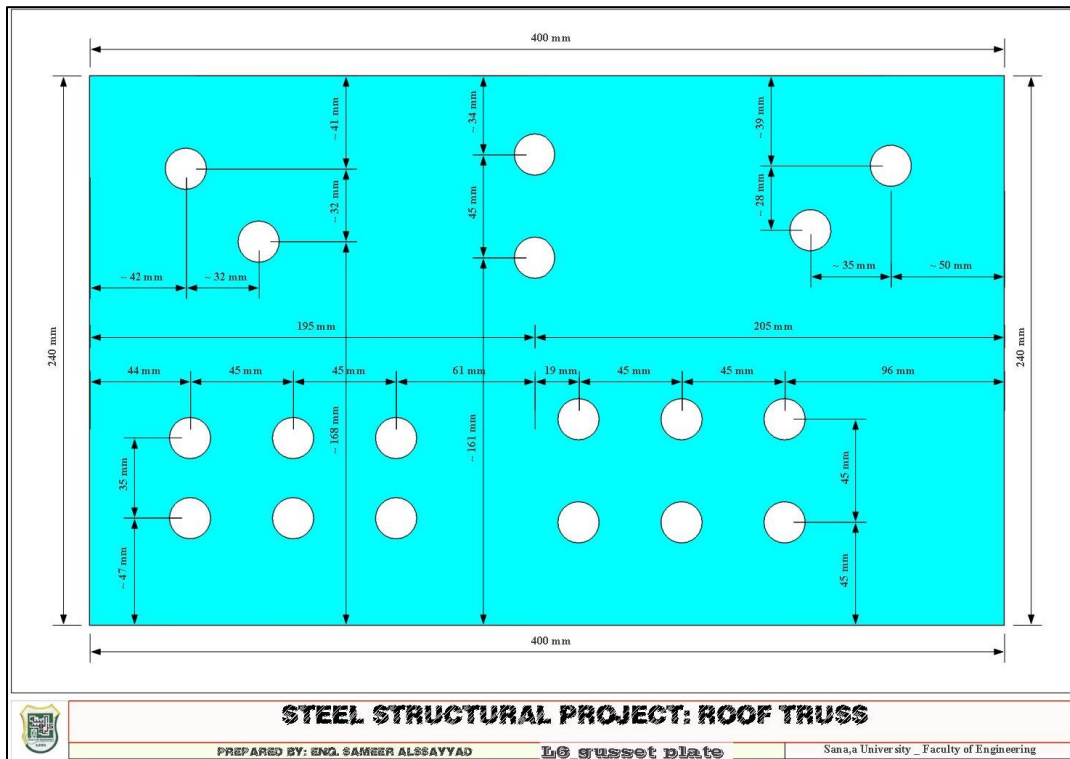
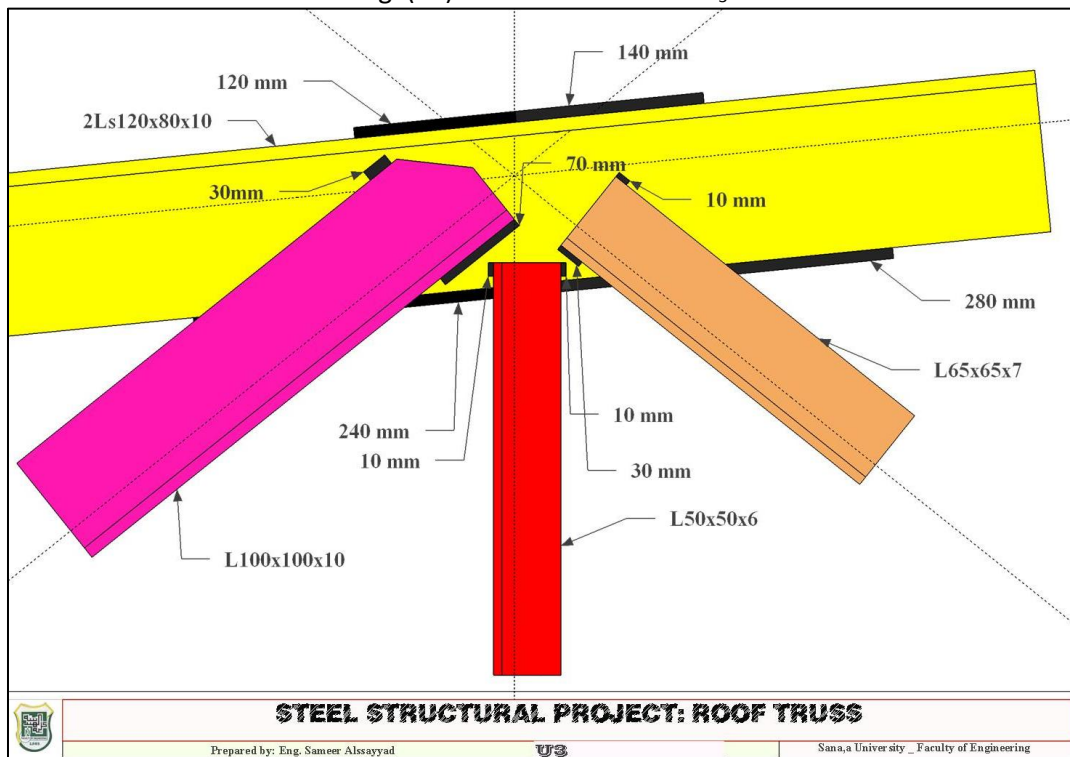


Fig. (18) Gusset plate for L<sub>6</sub>

Fig. (19) Welded connection U<sub>3</sub>



### **The bracing system of the building**

As we assumed the building doesn't use with vibration loading then we can use bracing in the upper chord only every four paws as shown in figures 2 and 3.

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